

# Stock Prices, News, and Economic Fluctuations

By PAUL BEAUDRY AND FRANCK PORTIER\*

There is a huge literature suggesting that stock price movements reflect the market's expectation of future developments in the economy. As a test of standard valuation models, Eugene F. Fama (1990) shows that monthly, quarterly, and annual stock returns are highly correlated with future production growth rates for the 1953–1987 period. This result is confirmed on a extended sample (1889–1988) by G. William Schwert (1990). Both authors argue that the relationship between current stock returns and future production growth reflects expectations about future cash flow that is impounded in stock prices. There is also a huge literature, and a long tradition in macroeconomics (from Arthur C. Pigou, 1927, and John Maynard Keynes, 1936, to the survey of Jess Benhabib and Roger E. A. Farmer, 1999) suggesting that changes in expectation may be an important element driving economic fluctuations.

Given this, it is surprising that the empirical macro literature—especially the VAR-based literature—rarely exploits stock price movements to expand our understanding of the role of expectations in business cycle fluctuations. In this paper, we take a step in this direction by showing how stock price movements, in conjunction with movements in total factor productivity (TFP), can be fruitfully used to help shed new light on the forces driving business cycle fluctuation.

The empirical strategy we adopt in this paper is to perform two different orthogonalization schemes as a means of identifying properties of

the data that can then be used to evaluate theories of business cycles. Let us be clear that our empirical strategy is a purely descriptive device which becomes of interest only when its implications are compared with those of structural models. The two orthogonalization schemes we use are based on imposing sequentially, not simultaneously, either impact or long-run restrictions on the orthogonalized moving average representation of the data. The primary system of variables that interests us is one composed of an index of stock market value and measured TFP. Our interest in focusing on stock market information is motivated by the view that stock prices are likely a good variable for capturing any changes in agents' expectations about future economic conditions.

The two disturbances we isolate with our procedure are: a disturbance that represents innovations in stock prices, which are orthogonal to innovations in TFP; and a disturbance that drives long-run movements in TFP. The main intriguing observation we uncover is that these two disturbances—when isolated separately without imposing orthogonality—are found to be almost perfectly colinear and to induce the same dynamics. We also show that these colinear shock series cause standard business cycle comovements and explain a large fraction of business cycle fluctuations. Moreover, when we use measures of TFP which control for variable rates of factor utilization, as, for example, when we use the series constructed by Basu et al. (2002), we find that our shock series anticipates TFP growth by several years.

In order to interpret the result from our empirical exercise, we present a model where technological innovations affect productive capacity with delay, and show how such a model can explain quite easily the patterns observed in the data. In particular, our evidence suggests that business cycles may be driven to a large extent by TFP growth that is heavily anticipated by economic agents, thereby leading to what might be called expectation-driven booms. Hence, our empirical results suggest that an important fraction of business cycle fluctuations may be driven by

\* Beaudry: CRC University of British Columbia, 997-1873 East Mall, Vancouver, BC, Canada V6T 1Z1, and National Bureau of Economic Research (e-mail: paulbe@interchange.ubc.ca); Portier: Université de Toulouse, 21 Allée de Brienne, F-31042 Toulouse, France (GREMAQ, IDEI, LEERNA, Institute Universitaire de France and CEPR) (e-mail: fportier@cict.fr). The authors thank Susanto Basu, Larry Christiano, Roger Farmer, Robert Hall, Richard Rogerson, Julio Rotemberg, and participants at seminars at CEPR ESSIM 2002, SED Paris 2003, Bank of Canada, Bank of England, the Federal Reserve of Philadelphia, the National Bureau of Economic Research, University of Berlin, Université du Québec à Montréal, Université de Toulouse, and CREST for helpful comments.

changes in expectations—as is often suggested in the macro literature—but these changes in expectations may well be based on fundamentals since they anticipate future changes in productivity.

The remaining sections of the paper are structured as follows. In Section I, we present our empirical strategy and show how it can be used to shed light on the sources of economic fluctuation. In Section II, we present the data and in Section III, we implement our strategy using postwar U.S. data. Finally, Section IV offers some concluding comments.

**I. Using Impact and Long-run Restrictions Sequentially to Learn About Macroeconomic Fluctuations**

The object of this section is to present a new means of using orthogonalization techniques—i.e., impact and long-run restrictions—to learn about the nature of business cycle fluctuations. Our idea is not to use these techniques simultaneously, but instead to use them sequentially. In particular, we will want to apply this sequencing to describe the joint behavior of stock prices (SP) and measured  $TFP_t$  in a manner that can be easily interpretable. The main characteristic of stock prices we want to exploit is that it is an unhindered jump variable.

*A. Two Orthogonalization Schemes*

Let us begin our discussion from a situation where we already have an estimate of the reduced form moving average (Wold) representation for the bivariate system  $(TFP_t, SP_t)$  (for ease of presentation we neglect any drift terms):

$$\begin{pmatrix} \Delta TFP_t \\ \Delta SP_t \end{pmatrix} = \mathbf{C}(L) \begin{pmatrix} \mu_{1,t} \\ \mu_{2,t} \end{pmatrix},$$

where  $L$  is the lag operator,  $\mathbf{C}(L) = \mathbf{I} + \sum_{i=1}^{\infty} \mathbf{C}_i L^i$ , and  $\mathbf{\Omega}$  is the variance covariance matrix of  $\mu$ . Furthermore, we assume that the system has at least one stochastic trend and therefore  $\mathbf{C}(1)$  is not equal to zero. In effect, most of our analysis will be based on a moving average representation derived from the estimation of a vector error correction model (VECM) for TFP and stock prices.

Now consider deriving from this Wold representation alternative representations with orthogonalized errors. As is well known, there are

many ways of deriving such representations. We want to consider two of these possibilities, one that imposes an impact restriction on the representation and one that imposes a long-run restriction. In order to see this clearly, let us denote these two alternative representations by

$$(1) \quad \begin{pmatrix} \Delta TFP_t \\ \Delta SP_t \end{pmatrix} = \mathbf{\Gamma}(L) \begin{pmatrix} \varepsilon_{1,t} \\ \varepsilon_{2,t} \end{pmatrix},$$

$$(2) \quad \begin{pmatrix} \Delta TFP_t \\ \Delta SP_t \end{pmatrix} = \tilde{\mathbf{\Gamma}}(L) \begin{pmatrix} \tilde{\varepsilon}_{1,t} \\ \tilde{\varepsilon}_{2,t} \end{pmatrix},$$

where  $\mathbf{\Gamma}(L) = \sum_{i=0}^{\infty} \mathbf{\Gamma}_i L^i$ ,  $\tilde{\mathbf{\Gamma}}(L) = \sum_{i=0}^{\infty} \tilde{\mathbf{\Gamma}}_i L^i$  and the variance covariance matrices of  $\varepsilon$  and  $\tilde{\varepsilon}$  are identity matrices. In order to get such a representation, say in the case of (1), we need to find the  $\mathbf{\Gamma}$  matrices that solve the following system of equations:

$$\begin{cases} \mathbf{\Gamma}_0 \mathbf{\Gamma}'_0 = \mathbf{\Omega} \\ \mathbf{\Gamma}_i = \mathbf{C}_i \mathbf{\Gamma}_0 \text{ for } i > 0. \end{cases}$$

Since this system has one more variable than equations, however, it is necessary to add a restriction to pin down a particular solution. In case (1), we do this by imposing that the 1, 2 element of  $\mathbf{\Gamma}_0$  is equal to zero; that is, we choose an orthogonalization where the second disturbance  $\varepsilon_2$  has no contemporaneous impact on  $TFP_t$ . In case (2), we impose that the 1, 2 element of the long-run matrix  $\tilde{\mathbf{\Gamma}}(1) = \sum_{i=0}^{\infty} \tilde{\mathbf{\Gamma}}_i$  equals zero; that is, we choose an orthogonalization where the disturbance  $\tilde{\varepsilon}_2$  has no long-run impact on  $TFP_t$  (the use of this type of orthogonalization was first proposed by Olivier Jean Blanchard and Danny Quah, 1989). We use these two different ways of organizing the data to help evaluate different classes of economic models and indicate directions for model reformulation. For example, a particular theory may imply that the correlation between the shocks  $\varepsilon_2$  and  $\tilde{\varepsilon}_1$  is close to zero and that their associated impulse responses are different. Therefore, we can evaluate the relevance of such a theory by examining the validity of its implications along such a dimension.

In order to clarify the potential usefulness of such a procedure, consider a simple canonical model of fluctuations driven by random walk technology shocks and random walk monetary shocks with orthogonal innovations  $\eta_{1,t}$  and  $\eta_{2,t}$ . The environment envisaged is a standard

New Keynesien model with monopolistic competition in the intermediate good sector and preset prices. The value of firms (the stock market value) in this economy is the discounted sum of profits of intermediate good producers. In such an economy, output and firm profits will be affected by unexpected money and the level of technology. Hence, as is easy to verify,<sup>1</sup> such a model delivers a structural moving average representation for  $TFP_t$  and stock market value ( $SP_t$ ) where the mapping between the structural shocks ( $\eta$ ) and the associated shocks ( $\varepsilon$  and  $\tilde{\varepsilon}$ ) is:

$$(3) \quad \varepsilon_1 = \eta_1, \quad \varepsilon_2 = \eta_2, \quad \tilde{\varepsilon}_1 = \eta_1, \quad \tilde{\varepsilon}_2 = \eta_2.$$

The important aspect of this model is that the derived  $\varepsilon_2$  shock, which under this theory should correspond to the money shock, is predicted to be orthogonal to  $\tilde{\varepsilon}_1$ , which should be the surprise increase in productivity. Therefore, looking at whether this type of pattern is found in the data provides a means of evaluating the relevance of such a class of models, that is, models where surprise technological disturbances are a potentially important source of fluctuations.

*A Model with Delayed Response of Innovation on Productivity.*—Let us now consider an alternative setting where stock prices continue to be a discounted sum of future profits, but where technological innovations no longer immediately increase productivity. Instead they only increase productive capacity over time. The objective of this example is to emphasize what such an environment predicts regarding the correlation between  $\varepsilon_2$  and  $\tilde{\varepsilon}_1$ , derived using sequential impact and long-run restrictions. To this end, let us assume that log TFP, denoted  $\theta$ , is composed of two components: a nonstationary component  $D_t$  and a stationary component  $\nu_t$ . The component  $\nu_t$  can be thought of either as a measurement error or as a temporary technology shock. For the discussion, we will treat  $\nu_t$  as a temporary shock to  $\theta$ , although the measurement error interpretation has the same implications. In contrast, the component  $D_t$  is the

permanent component of technology and is assumed to follow the process given below:

$$(4) \quad \begin{cases} \theta_t = D_t + \nu_t \\ D_t = \sum_{i=0}^{\infty} d_i \eta_{1,t-i} \\ d_i = 1 - \delta^i, \quad 0 \leq \delta < 1 \\ \nu_t = \rho \nu_{t-1} + \eta_{2,t}, \quad 0 \leq \rho < 1. \end{cases}$$

We will call the process for  $D_t$  a diffusion process, since an innovation  $\eta_1$  is restricted to have no immediate impact on productive capacity ( $d_0 = 0$ ), the effect of the technological innovation on productivity is assumed to grow over time ( $d_t \leq d_{t+1}$ ), and the long-run effect is normalized to one. In contrast to the common random walk assumption for the permanent component of TFP, such a process allows for an S-shaped response of TFP to a technological innovation. Now consider the implied structural moving average for  $\Delta TFP$  and  $\Delta SP$ , assuming that prices and wages are flexible, so that the only two innovations affecting real variables are the innovations to  $D_t$  and  $\nu_t$ . In this case, performing our short-run and long-run identification on this system, the relationship between the identified errors  $\varepsilon_t$ ,  $\tilde{\varepsilon}_t$  and the structural errors  $\eta_t$  are:

$$(5) \quad \varepsilon_1 = \eta_2, \quad \varepsilon_2 = \eta_1, \quad \tilde{\varepsilon}_1 = \eta_1, \quad \tilde{\varepsilon}_2 = \eta_2.$$

In particular, such a model predicts  $\varepsilon_2$  to be colinear to  $\tilde{\varepsilon}_1$ .

This diffusion model is different from a baseline New Keynesien model in that, even before technological opportunities have actually expanded an economy's production possibility set, forward-looking variables—such as stock prices—are incorporating this possibility. If this class of models is relevant, the long-run restriction used to derive the orthogonal moving average representation given by  $\tilde{\Gamma}_t$  and  $\tilde{\varepsilon}$  still implies that  $\tilde{\varepsilon}_1$  can be interpreted as a technological shock, but now it implies that this shock has zero effect on productivity on impact; that is, if productivity changes are anticipated, then by definition of an anticipated shock, the actual shock has zero effect on impact on  $TFP_t$ . Hence, under this type of model,  $\varepsilon_2$  and  $\tilde{\varepsilon}_1$  are predicted to be colinear as they both should capture the effect of anticipated changes in technological opportunities.

<sup>1</sup> See Beaudry and Portier (2004).

Moreover, the impulse responses associated with  $\varepsilon_2$  and  $\tilde{\varepsilon}_1$  should be identical.

## II. Data and Specification Issues

Our empirical investigation will use U.S. data over the period 1948-Q1 to 2000-Q4 (the data were collected in August 2002). The two series that interest us for our bivariate analysis are an index of stock market value (SP) and a measure of total factor productivity (TFP). Later, we will consider larger systems that also include consumption, investment, and hours worked, and therefore we also present the source of these data.

The stock market index we use is the quarterly Standards & Poors 500 Composite Stock Prices Index, deflated by the seasonally adjusted implicit price deflator of GDP in the nonfarm private business sector and transformed in per capita terms by dividing it by the population age 15 to 64. As the population series is annual, it has been interpolated assuming constant growth within the quarters of the same year. We denote the log of this index by  $SP$ .

The construction of our baseline TFP series is relatively standard. We restrict our attention to the nonfarm private business sector. From the U.S. Bureau of Labor Statistics (BLS), we retrieved two annual series: labor share ( $s_h$ ) and capital services ( $KS$ ), which measure the services derived from the stock of physical assets and software. The capital services series has been interpolated to obtain a quarterly series, assuming constant growth within the quarters of the same year. Output ( $Y$ ) and hours ( $H$ ) are quarterly and seasonally adjusted nonfarm business measures, from 1947-Q1 to 2000-Q4 (also from the BLS). We then construct a measure of (log) TFP as  $TFP_t = \log(Y_t / H_t^{\bar{s}_h} KS_t^{1-\bar{s}_h})$ , where  $\bar{s}_h$  is the average level of the labor share over the period.

The consumption measure ( $C$ ) we use is the per capita value of real personal consumption of nondurable goods and services, while investment ( $I$ ) is the per capita value of the sum of real personal consumption of durable goods and real fixed private domestic investment.

*Specification.*—From our data on TFP and SP, we first want to recover the Wold moving average representation for  $\Delta TFP$  and  $\Delta SP$ . Since from unit root tests (not reported here)

and cointegration tests, we found that  $SP$  and  $TFP$  are likely cointegrated  $I(1)$  processes, a natural means of recovering the Wold representation is by inverting a VECM. In a VECM framework, however, one must be careful to properly identify the matrix of cointegration relationships in order to avoid misspecification. In effect, as emphasized in James D. Hamilton (1994), if one is worried about potential misspecification, it may be best to estimate the VECM allowing for the matrix of cointegrating relationships to be of full rank—which corresponds to estimating the system in level. Then one can estimate the VECM with a matrix of cointegration relationships, which is of reduced rank, and examine whether the resulting Wold representation is similar to that found by estimating the system in levels. In the following, we adhere to this principal by reporting results based on a Wold representation achieved by inverting a VECM, having verified that the results are robust to estimating the system in levels. Since we want to avoid misspecification bias due to an omitted cointegration relationship, our approach to testing for a cointegrating relationship is conservative, in the sense of testing from a more (H0) cointegrating relationship to less (H1). To this end, we used the test proposed by Jukka Nyblom and Andrew Harvey (2000) to test for cointegration. This procedure indicates that cointegration between  $SP$  and  $TFP$  could not be rejected at the 5-percent level and therefore we adopted the VECM specification as our benchmark specification.

The second specification choice is related to the number of lags to include in the VECM. Again, our strategy is not to impose much on the data. According to the likelihood ratio test, two or five lags appear preferable—when testing in a descendant way for the optimal number of lags from two years up to one quarter. When testing one against the other, five is preferred to two. We therefore choose to work with five lags since this seemed to us large enough not to place too many restrictions on the data. It is, nevertheless, worth noting that all our results are robust to adopting a two-lag specification. One of the drawbacks of the way we have proceeded to choose this baseline specification is that we have examined the issues of cointegration rank and lag length sequentially. As has been shown by Søren Johansen (1992), such a procedure can have undesirable properties. As a

means of getting around this problem, John C. Chao and Peter C. B. Phillips (1999) propose a Posterior Information Criterion (PIC) that allows us to jointly select the lag length and cointegration rank of a VECM. The use of the PIC in the case at hand suggests a very parsimonious model with no cointegration and only one lag. The difference with the previous finding is not too surprising, since the PIC imposes a strong penalty for extra parameters. In order to select between the extremely parsimonious specification suggested using the PIC and the less restrictive specification discussed above, we performed a likelihood ratio test. Our finding was that specification selected by the PIC was rejected in favor of specifications with cointegration and more lags. Therefore, given our economic prior suggesting that TFP and stock prices are likely cointegrated, and given our desire not to impose unnecessary restrictions, we choose to proceed with the cointegration specification with five lags of data.<sup>2</sup>

### III. Results in a Bivariate System

#### A. Preliminary Results

We began by estimating a VECM for (*TFP*, *SP*) with one cointegrating relationship and recover two orthogonalized shock series corresponding to the  $\varepsilon$  and  $\tilde{\varepsilon}$  discussed in Section I, that is,  $\varepsilon$  was recovered by imposing an impact restriction (a restriction on  $\Gamma_0$ ) and  $\tilde{\varepsilon}$  was recovered by imposing a long-run restriction. The level impulse responses on (*TFP*, *SP*) associated with the  $\varepsilon_2$  shock and the  $\tilde{\varepsilon}_1$  shock are displayed in Figure 1. The striking observation is that these responses appear very similar when comparing one orthogonalization to another. More specifically, the dynamics associated with the  $\varepsilon_1$  shock—which by construction is an innovation in stock prices which are contemporaneously orthogonal to *TFP*—seem to permanently affect *TFP*, while the dynamics associated with the  $\tilde{\varepsilon}_1$  shock—which by construction has a permanent effect on *TFP*—have essentially no impact effect on *TFP* (the point estimate indicates a slight negative effect) but have a

substantial effect on *SP*. On the one hand, these results suggest that  $\varepsilon_2$  contains information about future TFP growth, which is instantaneously and positively reflected in stock prices.<sup>3</sup> On the other hand, they suggest that permanent changes in TFP are reflected in stock prices before they actually increase productive capacity.

The similarity between the effects of these two shocks derives from the quasi-identity of the  $\varepsilon_2$  shock and the  $\tilde{\varepsilon}_1$  shock, as shown in Figure 2, which simply plots  $\varepsilon_{2,t}$  against  $\tilde{\varepsilon}_{1,t}$ . In effect, the correlation coefficient between these two series is 0.97 (with a standard deviation of 0.006), that is, these two orthogonalization techniques recover essentially the same shock series.<sup>4</sup> The interesting question then becomes, what kind of structural macroeconomic model is consistent with these two orthogonalization techniques generating the same shock series? As we have discussed, this observation runs counter to simple models where technological improvements are modelled as surprises, since these models generally imply that  $\varepsilon_2$  and  $\tilde{\varepsilon}_1$  should be orthogonal. In contrast, this pattern appears consistent with the view—which we call the news view—that improvements in productivity are generally anticipated by market participants due to a lag between the recognition of a technological innovation and its eventual impact on productivity.<sup>5</sup>

Let us emphasize that, if we interpret the current results as reflecting a diffusion process from innovation to productivity, it suggest that diffusion is rather fast. In effect, in Figure 1 we observed that measured TFP starts growing quickly after the initial increase in stock prices, with the peak obtained after approximately four

<sup>3</sup> The observation in Figure 1, whereby *TFP* increases following an innovation in *SP*, indicates that stock prices Granger cause *TFP*. In effect, we also directly performed the test of whether *SP* Granger causes *TFP* in this system and we found that such causality could not be rejected at the 1-percent level.

<sup>4</sup> The observation that  $\varepsilon_2$  and  $\tilde{\varepsilon}_1$  are highly correlated suggests testing the overidentification restriction obtained by combining the short-run and long-run restrictions. When we perform this test within a minimum distance framework, we find that the overidentifying restriction is not rejected at conventional values ( $p$ -value = 0.90).

<sup>5</sup> In Beaudry and Portier (2004), we document the robustness of these observations to a different choice of lag length and to estimating the system in levels rather than in VECM form.

<sup>2</sup> Note that the type of models discussed in Section I generally implies that *SP*, and *TFP*, are cointegrated.

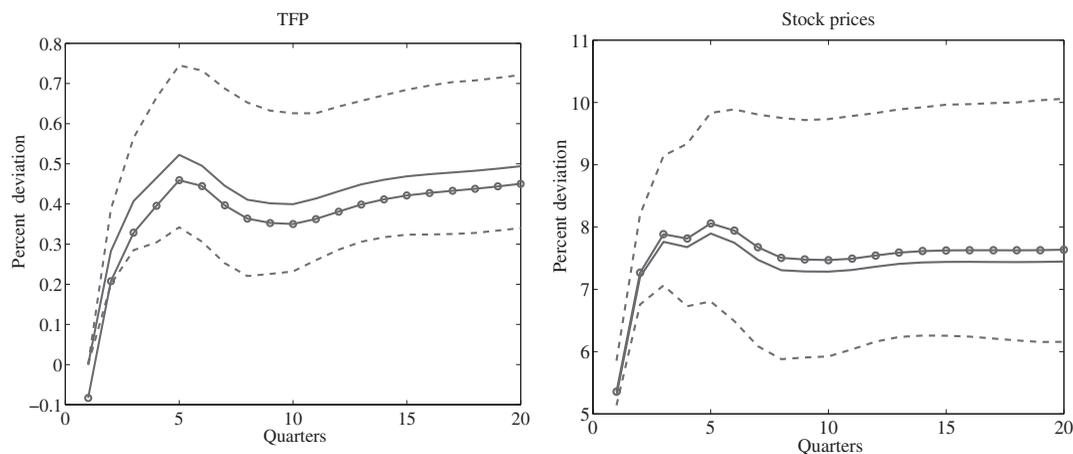


FIGURE 1. IMPULSE RESPONSES TO SHOCKS  $\varepsilon_2$  AND  $\tilde{\varepsilon}_1$  IN THE  $(TFP, SP)$  VECM

*Notes:* In both panels of this figure, the bold line represents the point estimate of the responses to a unit  $\varepsilon_2$  shock (the shock that does not have instantaneous impact of  $TFP$  in the short-run identification). The line with circles represents the point estimate of the responses to a unit  $\tilde{\varepsilon}_1$  shock (the shock that has a permanent impact on  $TFP$  in the long-run identification). Both identifications are done in the baseline bivariate specification (five lags and one cointegrating relation). The unit of the vertical axis is percentage deviation from the situation without shock. Dotted lines represent the 10-percent and 90-percent quantiles of the distribution of the impulse response functions (IRFs) in the case of the short-run identification, this distribution being the Bayesian simulated distribution obtained by Monte-Carlo integration with 2,500 replications, using the approach for just-identified systems discussed in Thomas J. Doan (1992).

quarters. One potential problem with this observation, however, is that our measure of  $TFP$  may be an improper measure of technological opportunities since it does not account for potential changes in rates of factor utilization. Therefore, it may be the case that in response to a technological innovation, properly measured  $TFP$  does not increase for a substantial period of time, but that mismeasured  $TFP$  responds rapidly due to changes in factor utilization. Hence, in the next subsection, we explore the robustness of our observations with respect to alternative measures of  $TFP$ .

### B. Controlling for Variable Rates of Factor Utilization

There is a vast literature regarding how best to calculate  $TFP$  in order to obtain a good reflection of changes in production opportunities. In particular, the literature on this issue emphasizes several potential problems with the type of measure of  $TFP$  we used in the previous section. For example, our previous measure may be inappropriate due to our lack of correction for variable rates of capital utilization, labor hoarding, or composition bias. One attempt to control for most of these biases can

be found in the  $TFP$  series produced by Susanto Basu et al. (2002) (hereafter BFK). This series has the advantage of being constructed from disaggregated data which control for variable rates of factor utilization. For this reason it appears as a good

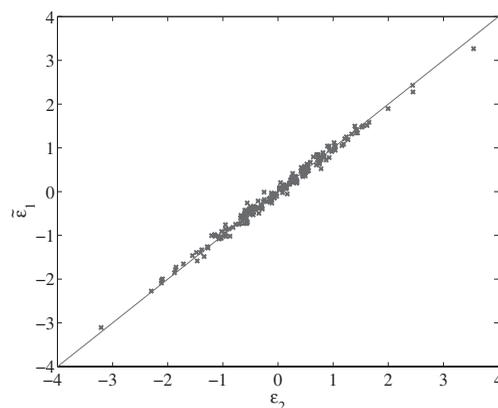


FIGURE 2. PLOT OF  $\varepsilon_2$  AGAINST  $\tilde{\varepsilon}_1$  IN THE  $(TFP, SP)$  VECM

*Notes:* This figure plots  $\varepsilon_2$  against  $\tilde{\varepsilon}_1$ . Both shocks are obtained from the baseline bivariate specification (five lags and one cointegrating relation). The straight line is the 45-degree line.

alternative series to examine the robustness of our previous results. It also has some drawbacks, however. First, it is an annual rather than quarterly series. Second, it covers only the period 1948 to 1989. Notwithstanding these drawbacks, we will begin this section by exploiting this series to see whether it changes any of our previous results. To this end, we estimated an annual bivariate VECM representation for stock prices and the BFK measure of TFP using three lags of data. The stock prices used are end-of-period prices. The results from sequentially imposing our impact and long-run restrictions to obtain orthogonal representations are given in Figures 3 and 4.

In Figure 3, we present the cross plot of  $\varepsilon_2$  and  $\tilde{\varepsilon}_1$  recuperated from the bivariate representation of TFP and SP using the BFK data. As can be seen, the two innovations are very highly correlated (0.989 with standard deviation 0.025), suggesting that both identification schemes isolate essentially the same shock.<sup>6</sup> In Figure 4, we present the impulse responses for *TFP* and *SP* associated with the innovations  $\varepsilon_2$  and  $\tilde{\varepsilon}_1$ . Although the responses to both these shocks are once again very similar, the response of *TFP* is quite different from our previous observations. In effect, we now see that following an increase in stock prices, TFP does not increase for several years. The point estimates actually suggest that TFP starts growing only four years after the initial rise in the stock market. This long lag between stock price increases and the increase in TFP is potentially consistent with a delayed impact of technological innovation on productivity, where the diffusion now appears quite slow, while it appeared to be rather quick with a less sophisticated measure of TFP.

As we indicated previously, there are two potential drawbacks with the BFK measure of TFP: it is annual and covers a limited period. As an alternative to the BFK measure, we constructed an adjusted TFP measure, which we will denote by  $TFP^A$ , using the BLS measure of capacity utilization ( $CU_t$ ) to adjust our measure of capital services. This adjusted TFP measure is calculated as  $TFP_t^A = \log(Y_t/H_t^{\bar{s}_h}(CU_tKS_t)^{1-\bar{s}_h})$ .

<sup>6</sup> The test of the overidentification restriction obtained by combining the long-run and short-run restrictions has a  $p$ -value of 0.83.

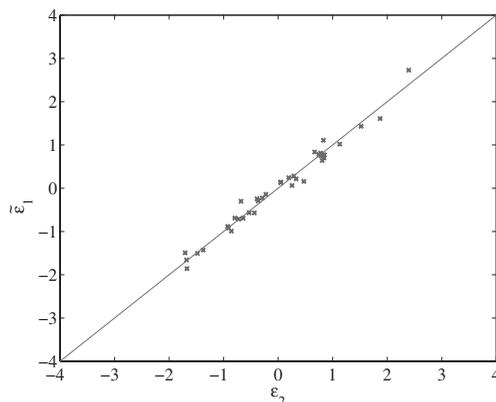


FIGURE 3. PLOT OF  $\varepsilon_2$  AGAINST  $\tilde{\varepsilon}_1$  IN THE (*TFP*, *SP*) VECM, USING BASU ET AL. (2002) MEASURE OF TFP (ANNUAL, 1949–1989)

Notes: This figure plots  $\varepsilon_2$  against  $\tilde{\varepsilon}_1$ . Both shocks are obtained from the baseline annual specification (two lags and one cointegrating relation). The straight line is the 45-degree line.

Since the BLS measure of capital utilization is based mainly on manufacturing data, this correction is not above criticism. Nevertheless, it is an alternative worth exploiting to see how results based on this data compare to those based on either the BFK data or on our unadjusted TFP data. In order to make these comparisons, we first performed our orthogonalizations on annual bivariate VAR over the period 1948 to 2000 using either the pair ( $TFP_t$ ,  $SP_t$ ) or ( $TFP_t^A$ ,  $SP_t$ ), where *TFP* refers to our original unadjusted TFP series, while  $TFP^A$  refers to our series adjusted for variable rates of factor utilization. In Figure 5, we superimpose the responses of TFP and stock prices to the orthogonalized shocks  $\varepsilon_2$  and  $\tilde{\varepsilon}_1$  estimated for each system. In the case where we use the annualized unadjusted TFP data, we see that measured TFP increases quickly after the innovation in stock prices, reaching a peak after two years, decreasing slightly afterward, and then resuming growth after about four years. This is quite similar to what was observed when the quarterly version of this data was used. In contrast, the results based on the TFP data adjusted for variations in the rate of capacity utilization ( $TFP^A$ ) are quite different from those based on unadjusted data, while interestingly they resemble the results obtained using the BFK data. In effect, we see that following the initial rise in stock prices,  $TFP^A$  does not overtake its initial

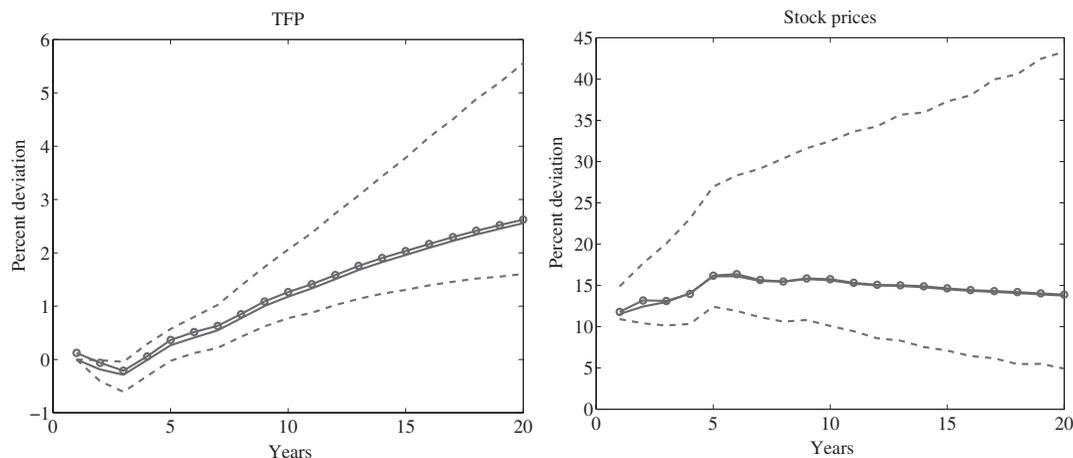


FIGURE 4. IMPULSE RESPONSES TO SHOCKS  $\varepsilon_2$  AND  $\tilde{\varepsilon}_1$  IN THE  $(TFP, SP)$  VECM, USING BASU ET AL. (2002) MEASURE OF TFP (ANNUAL, 1949–1989)

*Notes:* In both panels of this figure, the bold line represents the point estimate of the responses to a unit  $\varepsilon_2$  shock (the shock that does not have instantaneous impact on  $TFP$  in the short-run identification). The line with circles represents the point estimate of the responses to a unit  $\tilde{\varepsilon}_1$  shock (the shock that has a permanent impact on  $TFP$  in the long-run identification). Both identifications are done in the baseline annual specification (two lags and one cointegrating relation). The unit of the vertical axis is percentage deviation from the situation without shock. Dotted lines represent the 10-percent and 90-percent quantiles of the distribution of the  $IRF$  in the case of the short-run identification, this distribution being the Bayesian simulated distribution obtained by Monte-Carlo integration with 2,500 replications, using the approach for just-identified systems discussed in Doan (1992).

level before approximately three or four years, and this whether we are examining the response to  $\varepsilon_2$  or to  $\tilde{\varepsilon}_1$ . In effect, we once again observe that the responses of the different variables to an  $\varepsilon_2$  shock or to an  $\tilde{\varepsilon}_1$  shock are very similar, that is, the impact and long-run restrictions once again isolate essentially the same shock.<sup>7</sup> This is confirmed in Figure 6 where we provide a cross plot of  $\varepsilon_2$  against  $\tilde{\varepsilon}_1$  for both cases where the system is estimated annually using either the unadjusted  $TFP$  measure (correlation 0.98 with standard deviation 0.025) or the  $TFP$  measure adjusted for variable rates of capacity utilization (correlation 0.81 with standard deviation 0.083). In order to further confirm the similarities and differences associated with adjusting  $TFP$  using the BLS measure of capacity utilization, Figure 7 reports results based on quarterly data. In particular, in Figure 7, we report the responses of  $SP$  and  $TFP$  to an  $\varepsilon_2$  shock both for the case where  $TFP$  is unadjusted and for where it is adjusted. As can be seen, the response of

stock prices is almost unaffected by whether  $TFP$  is adjusted for variable utilization. In contrast, the short-run response of  $TFP$  depends once again on whether our measure of  $TFP$  is adjusted for variable utilization. In the case where  $TFP$  is adjusted for variable utilization, the growth response is substantially delayed relative to the case where  $TFP$  is unadjusted.

The results from using different measures of  $TFP$  suggest that our initial observation regarding the high correlation between  $\varepsilon_2$  and  $\tilde{\varepsilon}_1$  is very robust. In contrast, the timing of the response of  $TFP$  to such a shock depends heavily on whether  $TFP$  is adjusted for varying rates of capital utilization. In particular, when  $TFP$  is not adjusted for such a possibility, productivity appears to react quickly to the initial innovation in stock prices, which favors a quick diffusion interpretation. In contrast, when  $TFP$  is calculated either according to the disaggregated method of BFK or simply adjusted using the BLS measure of capacity utilization, the response of  $TFP$  is substantially delayed with the first signs of improvement not arising before three years. In our opinion, the substantially delayed responses associated with the adjusted

<sup>7</sup> This is confirmed by an overidentification restriction test.

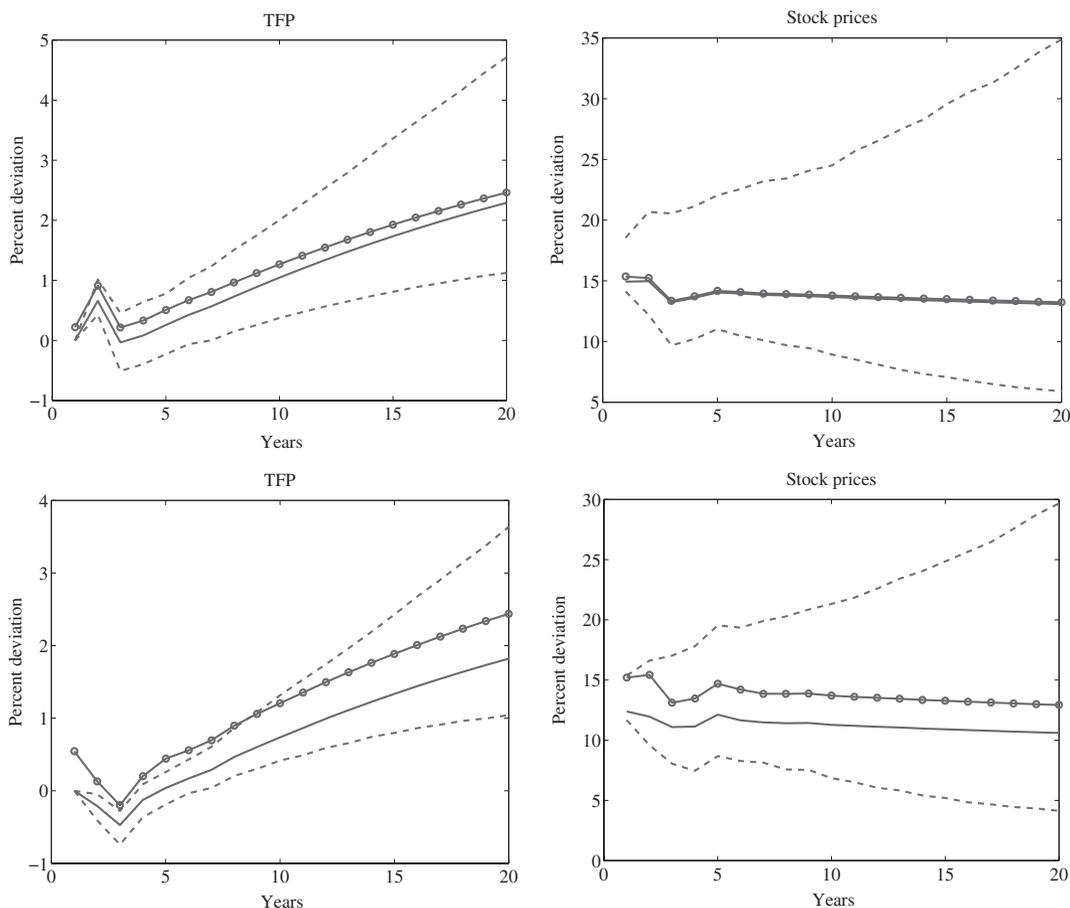


FIGURE 5. IMPULSE RESPONSES TO SHOCKS  $\varepsilon_2$  AND  $\bar{\varepsilon}_1$  IN THE  $(TFP, SP)$  VECM, USING ANNUAL OBSERVATIONS (1948–2000), WITHOUT ADJUSTING TFP FOR CAPACITY UTILIZATION (TOP PANELS) OR WITH TFP ADJUSTMENT (BOTTOM PANELS)

Notes: In each panel of this figure, the bold line represents the point estimate of the responses to a unit  $\varepsilon_2$  shock (the shock that does not have instantaneous impact on  $TFP$  in the short-run identification). The line with circles represents the point estimate of the responses to a unit  $\bar{\varepsilon}_1$  shock (the shock that has a permanent impact on  $TFP$  in the long-run identification). Both identifications are done in the baseline annual specification (two lags and one cointegrating relation). The unit of the vertical axis is percentage deviation from the situation without shock. Dotted lines represent the 10-percent and 90-percent quantiles of the distribution of the  $IRF$  in the case of the short-run identification, this distribution being the Bayesian simulated distribution obtained by Monte-Carlo integration with 2,500 replications, using the approach for just-identified systems discussed in Doan (1992).

measures of productivity constitute the more believable response to the actual changes in technology. We now examine whether this general pattern appears in higher dimensional systems.

#### IV. Higher Dimension Systems

In this section, we study systems in which—in addition to  $TFP$  and  $SP$ —consumption, hours worked, and investment are alternatively or jointly introduced. For each system, we show results that echo the results found in the bivariate case. All the

results we report in this section will be based, as in Section IIIA, on quarterly data over the period 1949 to 2000. Results based on yearly data give similar results.

##### A. A $(TFP, SP, C)$ System

Our approach here parallels that presented in Section I. Our objective is to sequentially impose orthogonalized restrictions on the moving average representation of  $(TFP, SP, C)$  as to derive, in one case, a shock that is contemporaneously

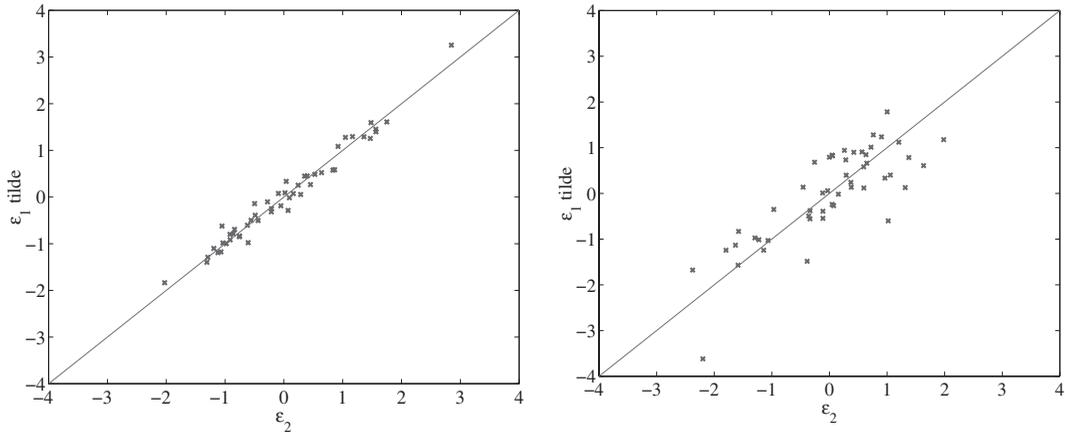


FIGURE 6. PLOT OF  $\varepsilon_2$  AGAINST  $\tilde{\varepsilon}_1$  IN THE  $(TFP, SP)$  VECM, USING ANNUAL OBSERVATIONS (1948–2000), WITHOUT ADJUSTING TFP FOR CAPACITY UTILIZATION (LEFT PANEL) OR WITH TFP ADJUSTMENT

Notes: Each panel of this figure plots  $\varepsilon_2$  against  $\tilde{\varepsilon}_1$ . Both shocks are obtained from the baseline annual specification (two lags and one cointegrating relation), with either  $TFP$  or  $TFP^A$ . The straight line is the 45-degree line.

orthogonal to  $TFP$ , while in the other case, to derive a shock that drives the long-run movements in  $TFP$ . Then, given these two shock series, we can examine whether they are highly correlated and whether they induce similar dynamics. The VECM for the system  $(TFP, SP, C)$  used in this section (i.e., the VECM used to derive the Wold representation) allows for two cointegrating relationships<sup>8</sup> and five lags.

Within this three-variable system, it is easy to derive the shock series that drives the long-run movements in  $TFP$ . This simply requires: (a) imposing the restriction that the 1, 2 and 1, 3 elements of the long-run matrix  $(\sum_{i=0}^{\infty} \tilde{\Gamma}_i(1))$  are equal to zero; and (b) recuperating the shock  $\tilde{\varepsilon}_1$ . In the case of recuperating the shock that is orthogonal to  $TFP$ , one must impose more structure. As in the bivariate case, we impose the impact restriction that the 1, 2 element of the impact matrix be equal to zero, and recuperate the associate shock  $\varepsilon_2$ . This is not sufficient to uniquely define  $\varepsilon_2$ , however. Having in mind that we would like our idea of a diffusion process to be embedded in an environment that allows for both a surprise technology shock and a temporary disturbance, we

impose no restrictions related to the shock  $\varepsilon_1$  as to let it potentially represent an unanticipated technology shock. As for the shock  $\varepsilon_3$ , we impose that it have no long-run effect on either TFP or consumption, and therefore can capture a temporary shock.<sup>9</sup>

<sup>9</sup> To understand this identification scheme, it is helpful to consider the following model of TFP:

$$TFP_t = R_t + D_t + v_t,$$

$$R_t = R_{t-1} + \eta_{1,t},$$

$$D_t = \sum_{i=0}^{\infty} d_i \eta_{2,t-i}, \quad d_0 = 0, \quad d_i \leq d_{i+1}, \quad \lim_{i \rightarrow \infty} d_i = 1,$$

$$v_t = \rho v_{t-1} + \eta_{3,t}, \quad 0 \leq \rho < 1.$$

In the case above, TFP is driven by three components: the first component is a random walk, the second a diffusion process (as we modelled previously), and the third a temporary disturbance (possibly a measurement error). If this is the data-generating process for  $TFP$  and these are the main shocks in the environment, then the structural impact matrix for a system composed of  $TFP, SP,$  and consumption will have a zero for its 1, 2 element (regardless of the precise theory for stock prices and consumption). Moreover, as long as the environment satisfies balanced growth and that stock prices continue to follow a martingale, then the third structural shock will have a zero long-run effect on both TFP and consumption. Hence, if the data-generating process satisfies these conditions, the recuperated  $\varepsilon_2$  shock should correspond to the innovation to the diffusion process (news).

<sup>8</sup> Using again the Nyblom and Harvery test, we found that these data do not reject two versus one cointegrating relationship at the 1-percent level, but do reject it at the 5-percent level. Since we want to be cautious with respect to possible misspecification bias, we choose to allow for two cointegrating relationships instead of one.

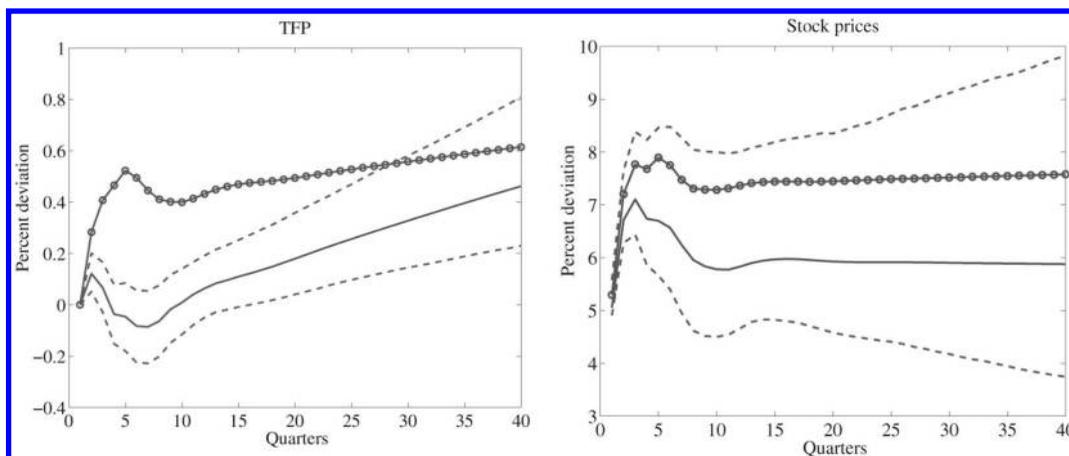


FIGURE 7. IMPULSE RESPONSES TO  $\varepsilon_2$  IN THE  $(TFP, SP)$  VECM, QUARTERLY DATA, WITH OR WITHOUT ADJUSTING FOR VARIABLE CAPACITY UTILIZATION

*Notes:* In both panels of this figure, the bold line represents the point estimate of the responses to a unit  $\varepsilon_2$  shock (the shock that does not have instantaneous impact on  $TFP$  in the short-run identification) in the VECM with adjusted  $TFP$ . The line with circles represents the point estimate of the responses to a unit  $\varepsilon_2$  shock in the VECM with nonadjusted  $TFP$ . The specification is the baseline bivariate one (five lags and one cointegrating relation). The unit of the vertical axis is percentage deviation from the situation without shock. Dotted lines represent the 10-percent and 90-percent quantiles of the distribution of the IRF in the VECM with adjusted  $TFP$ , this distribution being the Bayesian simulated distribution obtained by Monte-Carlo integration with 2,500 replications, using the approach for just-identified systems discussed in Doan (1992).

The impulse responses associated with the shocks  $\varepsilon_2$  and  $\tilde{\varepsilon}_1$  are presented in Figure 8. In this figure, we report results associated with estimating the system using either our baseline  $TFP$  measure or our measure adjusted for variable rates of capacity utilization. The identified shocks  $\varepsilon_2$  and  $\tilde{\varepsilon}_1$  are again found to be highly correlated, regardless of which measure of  $TFP$  is used: the correlation is 0.999 with standard deviation 0.002 with non-adjusted  $TFP$ , and the correlation is 0.92 with standard deviation 0.03 when we adjust for variable rates of capacity utilization. Moreover, Figure 8 indicates that these shocks induce similar dynamics and that the responses of consumption and stock prices to these shocks are barely affected by the measure of  $TFP$  used. Once again, however, we can notice that the timing of the response of  $TFP$  to both  $\varepsilon_2$  and  $\tilde{\varepsilon}_1$  depends heavily on the measure of  $TFP$  used. When we use the unadjusted measure,  $TFP$  starts increasing after one quarter. In contrast, with the adjusted  $TFP$  series, the short-run response is actually negative, and growth beyond its initial level takes somewhere between 12 and 16 quarters,

which is consistent with what we observed using the annual BFK data.<sup>10</sup>

### B. Four-Variable Systems

We now extend our analysis to a four-variable system where we begin by adding hours worked (in levels) to our system composed of  $TFP$ , stock prices, and consumption. Our objective is again to recuperate from one representation a shock (denoted  $\varepsilon_2$ ) that is an innovation in stock prices, which is orthogonal to  $TFP$ , and to recuperate

<sup>10</sup> Note that there are at least two simple mismeasurement interpretations of the initial negative response to adjusted  $TFP$  to either the  $\varepsilon_2$  or  $\tilde{\varepsilon}_1$  shock. The first is that our correction for varying capital utilization may be excessive, since it is based on high-cyclical manufacturing data. Hence, the adjusted  $TFP$  series may inherit a countercyclical bias. The second is that some investments, in learning, for example, may not be properly measured, leading to countercyclical bias if such investment is procyclical. In any case, given that all the results (adjusted or not) show that  $TFP$  is still approximately equal to its initial level of 12 to 16 quarters after the innovation in stock prices, the analysis strongly suggests that the real growth in  $TFP$  does not start until a few years after the initial innovation in stock prices.

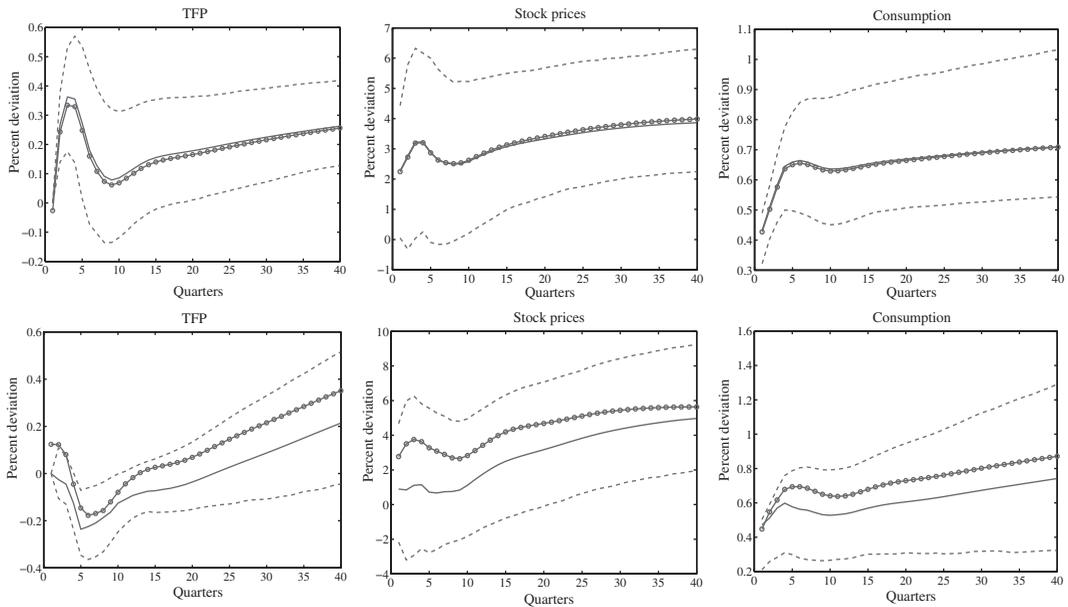


FIGURE 8. IMPULSE RESPONSES TO  $\varepsilon_2$  AND  $\tilde{\varepsilon}_1$  IN THE  $(TFP, SP, C)$  VECM, WITHOUT ADJUSTING TFP FOR CAPACITY UTILIZATION (UPPER PANELS) OR WITH TFP ADJUSTMENT (LOWER PANELS)

*Notes:* In each panel of this figure, the bold line represents the point estimate of the responses to a unit  $\varepsilon_2$  shock (the shock that does not have instantaneous impact on *TFP* in the short-run identification). The line with circles represents the point estimate of the responses to a unit  $\tilde{\varepsilon}_1$  shock (the shock that has a permanent impact on *TFP* in the long-run identification). Both identifications are done in the baseline trivariate specification (five lags and two cointegrating relations). The unit of the vertical axis is percentage deviation from the situation without shock. Dotted lines represent the 10-percent and 90-percent quantiles of the distribution of the IRF in the case of the short-run identification, this distribution being the Bayesian simulated distribution obtained by Monte-Carlo integration with 2,500 replications, using the approach for just-identified systems discussed in Doan (1992).

from another representation a shock (denoted  $\tilde{\varepsilon}_1$ ) that is associated with permanent movements in *TFP*. The  $\tilde{\varepsilon}_1$  shock can be isolated by imposing that the long-run matrix  $\tilde{\Gamma}(1)$  be lower triangular. In order to isolate the shock  $\varepsilon_2$ , we impose: (a) no restriction related to the shock  $\varepsilon_1$  as to allow it to potentially capture a traditional surprise productivity shock; (b) that the 1, 2 element of the impact matrix  $\Gamma_0$  be zero to assure that  $\varepsilon_2$  is not contemporaneously correlated with *TFP*; (c) as before, that the first and third elements of the third column of the long-run matrix be zero, to potentially allow  $\varepsilon_3$  to be a temporary shock to technology; and (d) that  $\varepsilon_4$  is an hours specific shock, i.e., that there are zeros in the first three elements of the last column of the impact matrix (this last shock can be interpreted as a measurement error in hours worked).

Figure 9 displays the response of the four variables to the shocks  $\varepsilon_2$  and  $\tilde{\varepsilon}_1$ . As in the case of the three-variable system, we once again report results based on using our unadjusted

*TFP* measure, as well as our adjusted measure. Although not displayed, the cross-plot of  $\varepsilon_2$  against  $\tilde{\varepsilon}_1$  looks similar to the previous plots; we observe a very high correlation (0.993 with a standard deviation of 0.008 with no adjustment of *TFP*, 0.990 standard deviation 0.01 with adjustment).

There are three aspects worth noticing in Figure 9. First, the responses of consumption, hours, and stock prices are very similar regardless of the measure of *TFP* used. Second, there is a substantial hump-shaped response of hours to either the shock  $\varepsilon_2$  or  $\tilde{\varepsilon}_1$ . In particular, this hump response lasts about 10 to 12 quarters, with the hump being echoed mildly in consumption.<sup>11</sup> Finally, as before, the timing of the

<sup>11</sup> The observed positive response of hours worked to a shock that permanently changes productivity presented in Figure 9 runs counter to the results presented in Jordí Gali (1999), but is consistent with the results presented in Laurence J. Christiano et al. (2003).

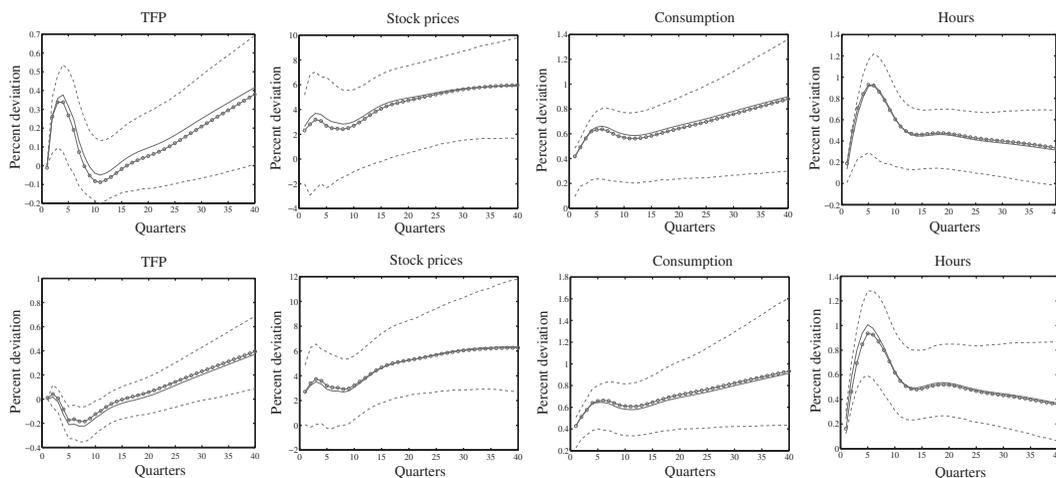


FIGURE 9. IMPULSE RESPONSES TO  $\varepsilon_2$  AND  $\bar{\varepsilon}_1$  IN THE  $(TFP, SP, C, H)$  VECM, WITHOUT (UPPER PANELS) OR WITH (LOWER PANELS) ADJUSTING TFP FOR CAPACITY UTILIZATION

*Notes:* In each panel of this figure, the bold line represents the point estimate of the responses to a unit  $\varepsilon_2$  shock (the shock that does not have instantaneous impact on  $TFP$  in the short-run identification). The line with circles represents the point estimate of the responses to a unit  $\bar{\varepsilon}_1$  shock (the shock that has a permanent impact on  $TFP$  in the long-run identification). In this system with hours, both identifications are done in a specification with five lags and three cointegrating relations, i.e., a VAR in levels. The unit of the vertical axis is percentage deviation from the situation without shock. Dotted lines represent the 10-percent and 90-percent quantiles of the distribution of the IRF in the case of the short-run identification, this distribution being the Bayesian simulated distribution obtained by Monte-Carlo integration with 2,500 replications, using the approach for just-identified systems discussed in Doan (1992).

response of  $TFP$  depends heavily on the measure of  $TFP$  used. When we use our adjusted measure of  $TFP$  ( $TFP^A$ ), growth in  $TFP$  above its initial level arises only 12 to 15 quarters after the initial jump in stock prices. In contrast, in the case where we use our unadjusted measure of  $TFP$ , measured productivity appears to go through a temporary boom, which is precisely what is expected if there are important cyclical variations in the rate of capital utilization. It is also interesting to note that the permanent growth in  $TFP$  arrives after the period of a temporary boom in consumption and hours. In this sense, this way of looking at the data isolates a burst in economic activity that predates the pick-up in  $TFP$  growth. In effect, what is noticeable about the impulse responses in Figure 9 is the rich dynamics over the first two to three years. During this period, the economy appears to go through an important temporary boom, then a slight recession, followed by a period of substantial  $TFP$  growth. Given a technological-diffusion interpretation of this shock, this temporary boom period may result from a period of time when agents in the economy try

best to position themselves to take advantage of future technological change.

In order to evaluate the importance of this phenomenon in business cycles, Figure 10 reports the variance decompositions for consumption ( $C$ ), investment ( $I$ ), output ( $C + I$ ), and hours worked ( $H$ ) for the  $\varepsilon_2$  and  $\bar{\varepsilon}_1$  shocks retrieved from the system based on either the adjusted or unadjusted measure of  $TFP$ . In order to calculate the variance decomposition for output and investment, we replaced hours worked in the four-variable VAR by investment or output. The impulse responses associated with these two latter exercises are not reported since they look similar to those in Figure 9.

The variance decompositions in Figure 10 indicate that  $\varepsilon_2$ , and similarly  $\bar{\varepsilon}_1$ , explain a substantial fraction of fluctuations at business cycle frequencies. In effect, given the interpretation of this shock as reflecting news about technological innovations, the variance decomposition results suggest that news shocks may be a major source of business cycle fluctuations, even if surprise changes in productivity may not be. Let us note that the second part of this observation

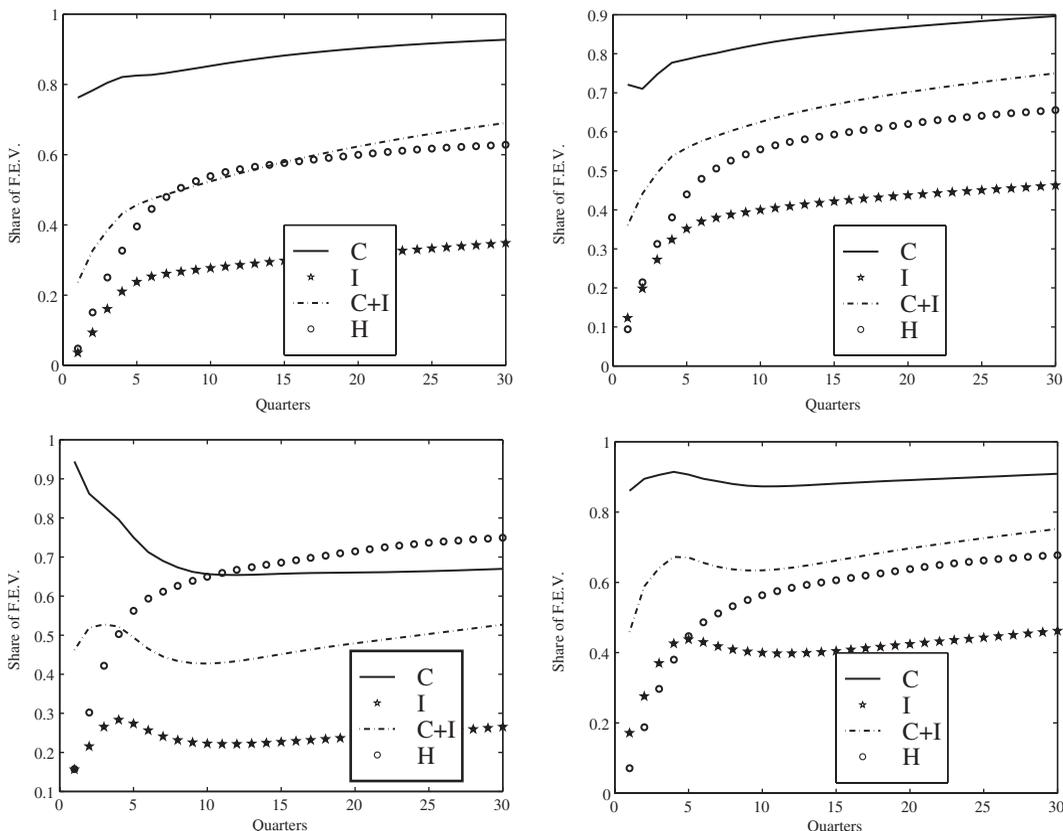


FIGURE 10. SHARE OF THE FORECAST ERROR VARIANCE (F.E.V.) OF CONSUMPTION (C), INVESTMENT I, OUTPUT (C + I), AND HOURS (H) ATTRIBUTABLE TO  $\epsilon_2$  (LEFT PANELS) AND TO  $\tilde{\epsilon}_1$  (RIGHT PANELS) IN VECMS, WITH NONADJUSTED TFP (TOP PANELS) OR ADJUSTED TFP (BOTTOM PANELS)

Notes: This figure has four panels. The left panels display the share of the forecast variance of consumption and investment that is attributable to  $\epsilon_2$  (short-run identification) in the  $(TFP, SP, C, I)$  VECM (five lags and three cointegrating relations), of output  $(C + I)$  in the  $(TFP, SP, C, C + I)$  VECM (five lags and three cointegrating relations), and of hours  $(H)$  in the  $(TFP, SP, C, H)$  VECM (five lags and four cointegrating relations, i.e., a VAR in levels). The right panels display the same information in the case of the shock  $\tilde{\epsilon}_1$  (long-run identification). The top row uses a nonadjusted measure of TFP, while TFP is adjusted for variable capacity utilization in the bottom row.

is consistent with the findings of Basu et al. (2002) and others, who have recently questioned the relevance of surprise changes in productivity as a driving force behind business cycles.

#### IV. Conclusion

In this paper, we have presented properties of the joint behavior of total factor productivity and stock prices which highlight new challenges for business cycle theory. In particular, we presented two orthogonalized moving average representations for these variables: one

based on an impact restriction and one based on a long-run restriction. We then examined the correlation between the innovations that drive the long-run movements in  $TFP$  and the innovation which is contemporaneously orthogonal to  $TFP$ . We found this correlation to be positive and almost equal to one, indicating that permanent changes in productivity growth are preceded by stock market booms. We showed why this observed positive correlation runs counter to that predicted by simple models where surprise changes in productivity drive fluctuations. We also discussed how the pattern could arise if agents advanced information about future tech-

nological opportunities. The results suggest that changes in technological opportunities may be central to business cycle fluctuations, even if surprise changes in productivity are not. Hence, these observations highlight the potential fruitfulness of reexamining the manner in which productivity growth is modelled in business cycle analysis. In particular, the type of model that is needed to explain the observations is one where agents recognize changes in technological opportunities well in advance of their effect on productivity, and where the recognition itself leads to a boom in both consumption and investment, which precedes the growth in productivity.

#### REFERENCES

- Basu, Susanto; Fernald, John and Kimball, Miles.** "Are Technology Improvements Contractionary?" National Bureau of Economic Research, Inc., NBER Working Papers: No. 10592, 2004.
- Beaudry, Paul and Portier, Franck.** "Stock Prices, News and Economic Fluctuations." National Bureau of Economic Research, Inc., NBER Working Papers: No. 10548, 2004.
- Benhabib, Jess and Farmer, Roger E. A.** "Indeterminacy and Sunspots in Macroeconomics," in John B. Taylor and Michael Woodford, eds., *Handbook of macroeconomics*. Vol. 1A. Amsterdam: Elsevier Science, North-Holland, 1999, pp. 387–448.
- Blanchard, Olivier Jean and Quah, Danny.** "The Dynamic Effects of Aggregate Demand and Supply Disturbances." *American Economic Review*, 1989, 79(4), pp. 655–73.
- Chao, John C. and Phillips, Peter C. B.** "Model Selection in Partially Nonstationary Vector Autoregressive Processes with Reduced Rank Structure." *Journal of Econometrics*, 1999, 91(2), pp. 227–71.
- Christiano, Lawrence J.; Eichenbaum, Martin and Vigfusson, Robert.** "What Happens after a Technology Shock?" U.S. Federal Reserve Board, International Finance Discussion Papers: No. 768, 2003.
- Doan, Thomas J.** *RATS manual*. Evanston, IL: Estima, 1992.
- Fama, Eugene F.** "Stock Returns, Expected Returns, and Real Activity." *Journal of Finance*, 1990, 45(4), pp. 1089–1108.
- Gali, Jordi.** "Technology, Employment, and the Business Cycle: Do Technology Shocks Explain Aggregate Fluctuations?" *American Economic Review*, 1999, 89(1), pp. 249–71.
- Hamilton, James D.** *Time series analysis*. Princeton: Princeton University Press, 1994.
- Johansen, Søren.** "Determination of Cointegrating Rank in the Presence of a Linear Trend." *Oxford Bulletin of Economics and Statistics*, 1992, 54(3), pp. 383–97.
- Keynes, John Maynard.** *The general theory of employment, interest and money*. London: Macmillan, 1936.
- Nyblom, Jukka and Harvey, Andrew.** "Tests of Common Stochastic Trends." *Econometric Theory*, 2000, 16(2), pp. 176–99.
- Pigou, Arthur C.** *Industrial fluctuations*. London: Macmillan, 1927.
- Schwert, G. William.** "Stock Returns and Real Activity: A Century of Evidence." *Journal of Finance*, 1990, 45(4), pp. 1237–57.