

## **Application:** Stock-Watson (*JEP* 2001)

$$\mathbf{A} \begin{pmatrix} \pi_t \\ U_t \\ R_t \end{pmatrix} = \mathbf{C}(L) \begin{pmatrix} \pi_{t-1} \\ U_{t-1} \\ R_{t-1} \end{pmatrix} + \begin{pmatrix} v_t^1 \\ v_t^2 \\ v_t^P \end{pmatrix}$$

Workfile: SW\_JEP01 - (c:\bagliano\corsi\monet2\var\sw\_jep01.wf1) - □ X

View Proc Object Save Freeze Details+/- Show Fetch Store Delete Genr Sample

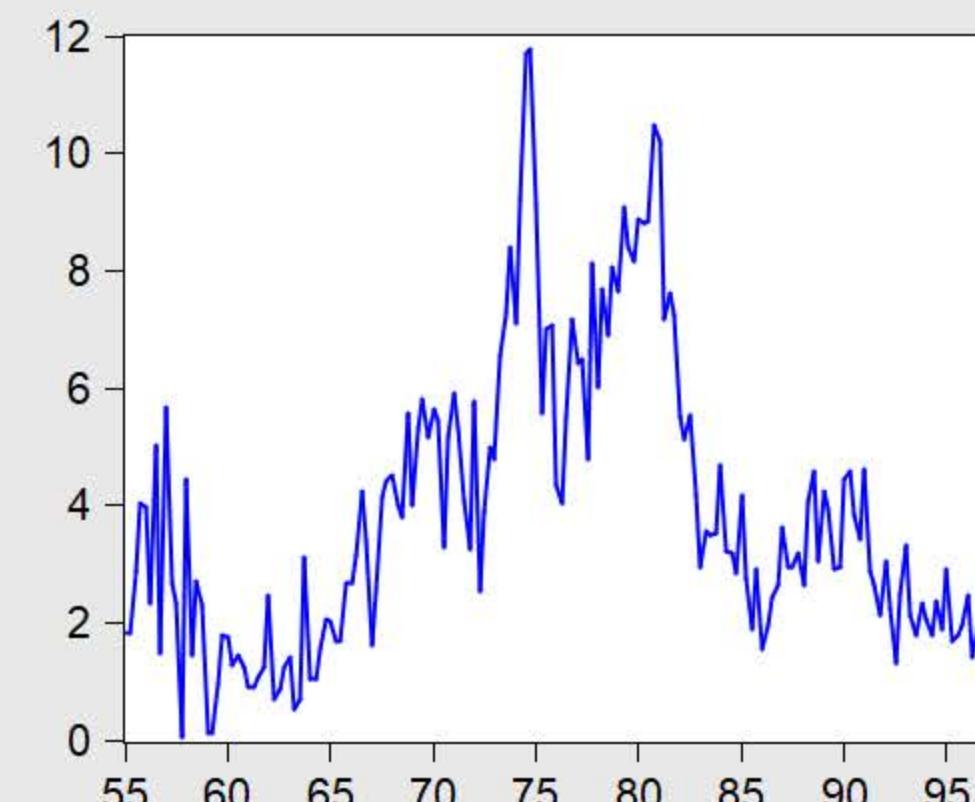
Range: 1955Q1 2000Q4 -- 184 obs Filter: \*

Sample: 1955Q1 2000Q4 -- 184 obs Order: Name

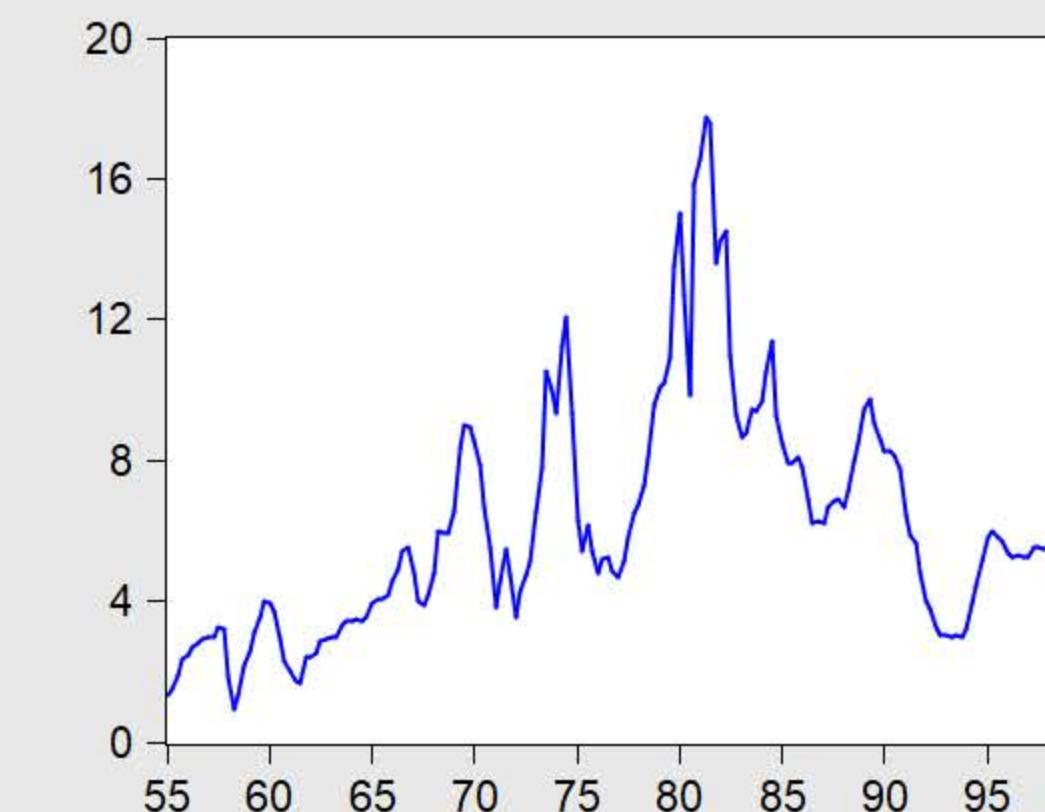
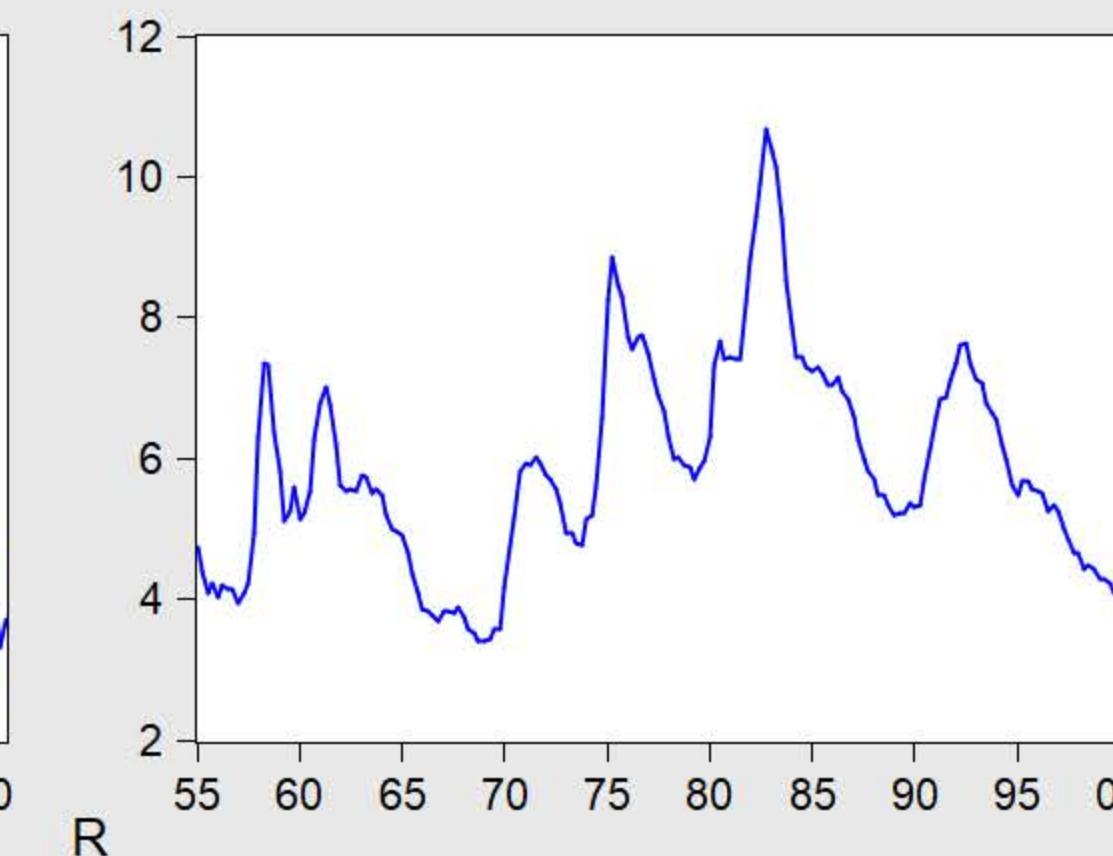
c  
 infl  
 r  
 resid  
 u

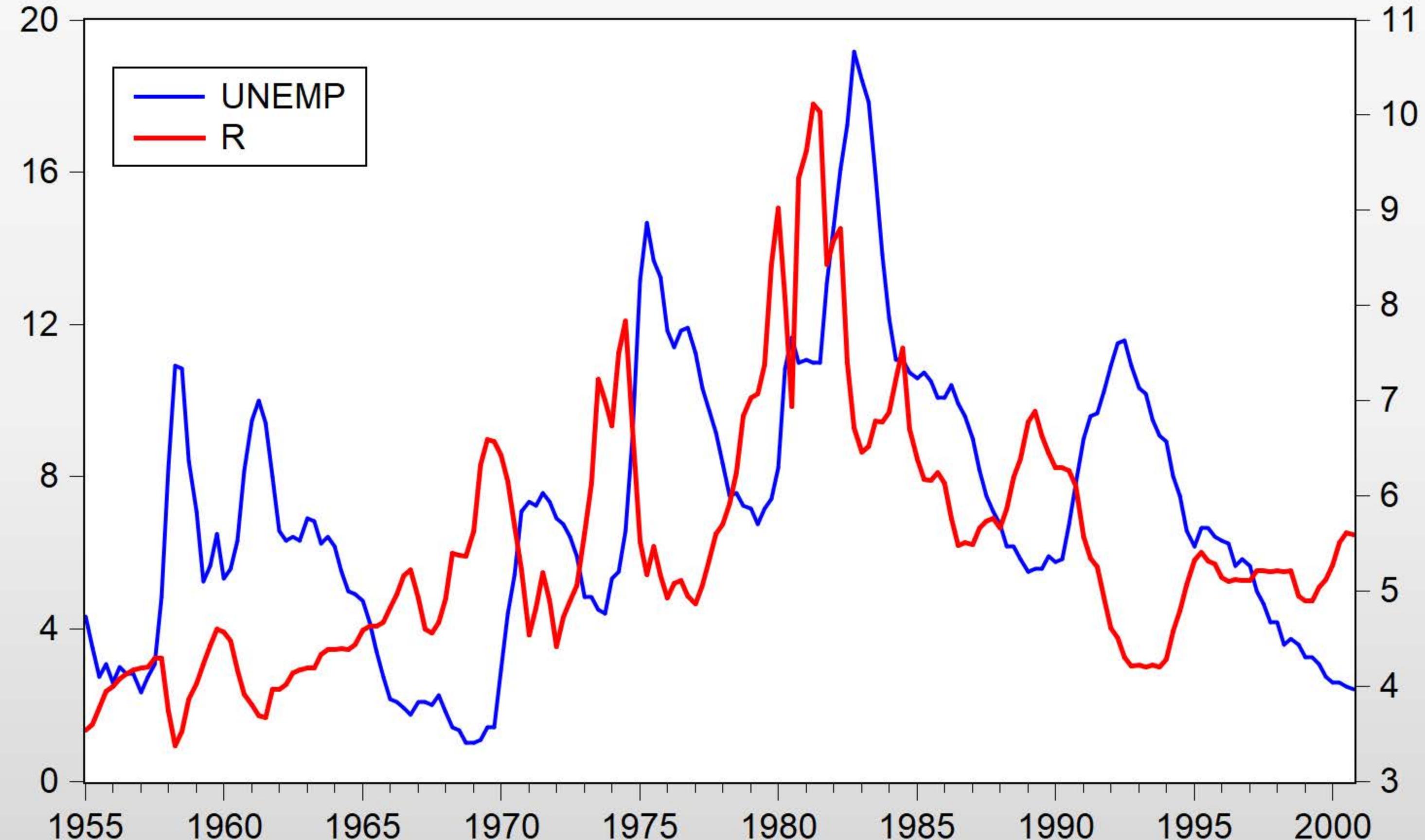
< > \ StockWatson\_data \ VAR\_analysis \ New Page /

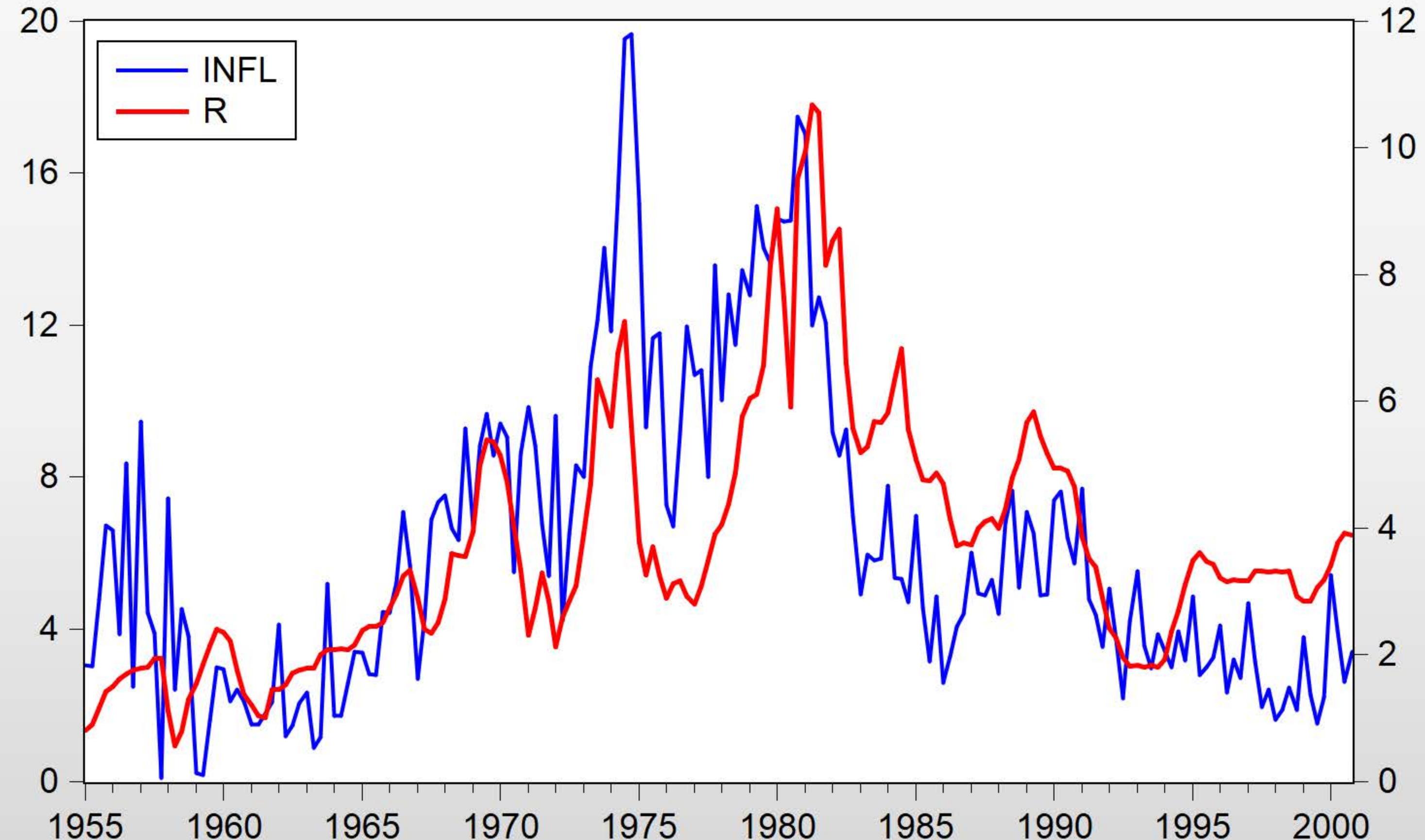
INFL



UNEMP







EViews

File Edit Object View Proc Quick Options Add-ins Window Help

Workfile: SW\_JEP01 - (c:\bagliano\corsi\monet2\var\sw\_jep01.wf1)

View Proc Object Save Freeze Details+/- Show Fetch Store Delete Genr Sample

Range: 1955Q1 2000Q4 -- 184 obs Filter: \*

Sample: 1955Q1 2000Q4 -- 184 obs Order: Name

c  
corr\_inn  
endog  
fevd\_12  
fevd\_120  
infl  
infl\_r  
irf\_40  
r  
resid  
u\_infl  
u\_r  
u\_unemp  
unemp  
unemp\_r  
v2  
var  
var4  
vp

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VAR Specification

Basics

VAR Type

Unrestricted VAR  
 Vector Error Correction  
 Bayesian VAR

Endogenous Variables

infl unemp r

Estimation Sample

1960q1 2000q4

Lag Intervals for Endogenous:

1 4

Exogenous Variables

c

OK Annulla

Path = c:\users\fabio bagliano\dropbox (esomas)\econometrics - historical papers\di fenizio DB = none WF = sw\_jep01

14:13 13/09/2022

Workfile: SW\_JEP01 - (c:\baglano\corsi\monet2\var\sw\_jep01.wf1)

View Proc Object Save Freeze Details+/- Show Fetch Store Delete Genr Sample

Range: 1955Q1 2000Q4 -- 184 obs Filter: \*

Sample: 1955Q1 2000Q4 -- 184 obs Order: Name

- c
- corr\_inn
- endog
- fevd\_12
- fevd\_120
- infl
- infl\_r
- irf\_40
- r
- resid
- u\_infl
- u\_r
- u\_unemp
- unemp
- unemp\_r
- v2
- var4
- vp

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Var: UNTITLED Workfile: SW\_JEP01::VAR\_analysis

View Proc Object Print Name Freeze Estimate Stats Impulse Resids

Vector Autoregression Estimates

**Vector Autoregression Estimates**

**Date: 09/13/22 Time: 14:35**

**Sample: 1960Q1 2000Q4**

**Included observations: 164**

**Standard errors in ( ) & t-statistics in [ ]**

|           | INFL                                | UNEMP                                | R                                    |
|-----------|-------------------------------------|--------------------------------------|--------------------------------------|
| INFL(-1)  | 0.546602<br>(0.07866)<br>[ 6.94890] | 0.030733<br>(0.01870)<br>[ 1.64377]  | 0.086682<br>(0.06935)<br>[ 1.24984]  |
| INFL(-2)  | 0.075629<br>(0.08941)<br>[ 0.84583] | -0.030821<br>(0.02125)<br>[-1.45026] | 0.193629<br>(0.07884)<br>[ 2.45610]  |
| INFL(-3)  | 0.111728<br>(0.09006)<br>[ 1.24052] | 0.029789<br>(0.02141)<br>[ 1.39157]  | -0.078252<br>(0.07941)<br>[-0.98541] |
| INFL(-4)  | 0.266606<br>(0.08228)<br>[ 3.24007] | -0.024084<br>(0.01956)<br>[-1.23145] | -0.027216<br>(0.07255)<br>[-0.37514] |
| UNEMP(-1) | -0.938366                           | 1.484507                             | -1.565494                            |

Workfile: SW\_JEP01 - (c:\bagliano\corsi\monet2\var\sw\_jep01.wf1)

View Proc Object Save Freeze Details+/- Show Fetch Store Delete Genr Sample

Range: 1955Q1 2000Q4 -- 184 obs Filter: \*

Sample: 1955Q1 2000Q4 -- 184 obs Order: Name

- c
- corr\_inn
- endog
- fevd\_12
- fevd\_120
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- infl\_r
- irf\_40
- r
- resid
- u\_infl
- u\_r
- u\_unemp
- unemp
- unemp\_r
- v2
- var4
- vp

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Var: UNTITLED Workfile: SW\_JEP01::VAR\_analysis

View Proc Object Print Name Freeze Estimate Stats Impulse Resids

Vector Autoregression Estimates

|                  | [ -2.99914 ]                                 | [ -0.99274 ]                                 | [ -1.91050 ]                                 |
|------------------|--|--|--|
| <b>UNEMP(-4)</b> | <b>0.587782</b><br>(0.34458)<br>[ 1.70581]   | <b>-0.053440</b><br>(0.08190)<br>[ -0.65250] | <b>0.626826</b><br>(0.30381)<br>[ 2.06321]   |
| <b>R(-1)</b>     | <b>0.227701</b><br>(0.10046)<br>[ 2.26651]   | <b>-0.003358</b><br>(0.02388)<br>[ -0.14061] | <b>0.948524</b><br>(0.08858)<br>[ 10.7084]   |
| <b>R(-2)</b>     | <b>-0.228725</b><br>(0.13458)<br>[ -1.69956] | <b>0.050389</b><br>(0.03199)<br>[ 1.57529]   | <b>-0.381030</b><br>(0.11866)<br>[ -3.21117] |
| <b>R(-3)</b>     | <b>0.062624</b><br>(0.13390)<br>[ 0.46768]   | <b>-0.020360</b><br>(0.03183)<br>[ -0.63971] | <b>0.332095</b><br>(0.11806)<br>[ 2.81287]   |
| <b>R(-4)</b>     | <b>-0.069266</b><br>(0.10242)<br>[ -0.67630] | <b>0.005464</b><br>(0.02434)<br>[ 0.22444]   | <b>0.029857</b><br>(0.09030)<br>[ 0.33064]   |
| <b>C</b>         | <b>1.027154</b><br>(0.37358)<br>[ 2.74946]   | <b>0.101297</b><br>(0.08880)<br>[ 1.14079]   | <b>0.505753</b><br>(0.32939)<br>[ 1.53544]   |

Workfile: SW\_JEP01 - (c:\baglano\corsi\monet2\var\sw\_jep01.wf1)

View Proc Object Save Freeze Details+/- Show Fetch Store Delete Genr Sample

Range: 1955Q1 2000Q4 -- 184 obs Filter: \*

Sample: 1955Q1 2000Q4 -- 184 obs Order: Name

c  
 corr\_inn  
 endog  
 fevd\_12  
 fevd\_120  
 infl  
 infl\_r  
 irf\_40  
 r  
 resid  
 u\_infl  
 u\_r  
 u\_unemp  
 unemp  
 unemp\_r  
 v2  
 var4  
 vp

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[var] Var: UNTITLED Workfile: SW\_JEP01::VAR\_analysis

View Proc Object Print Name Freeze Estimate Stats Impulse Resids

VAR Stability Condition Check

## Roots of Characteristic Polynomial

**Endogenous variables: INF UNEMP R**

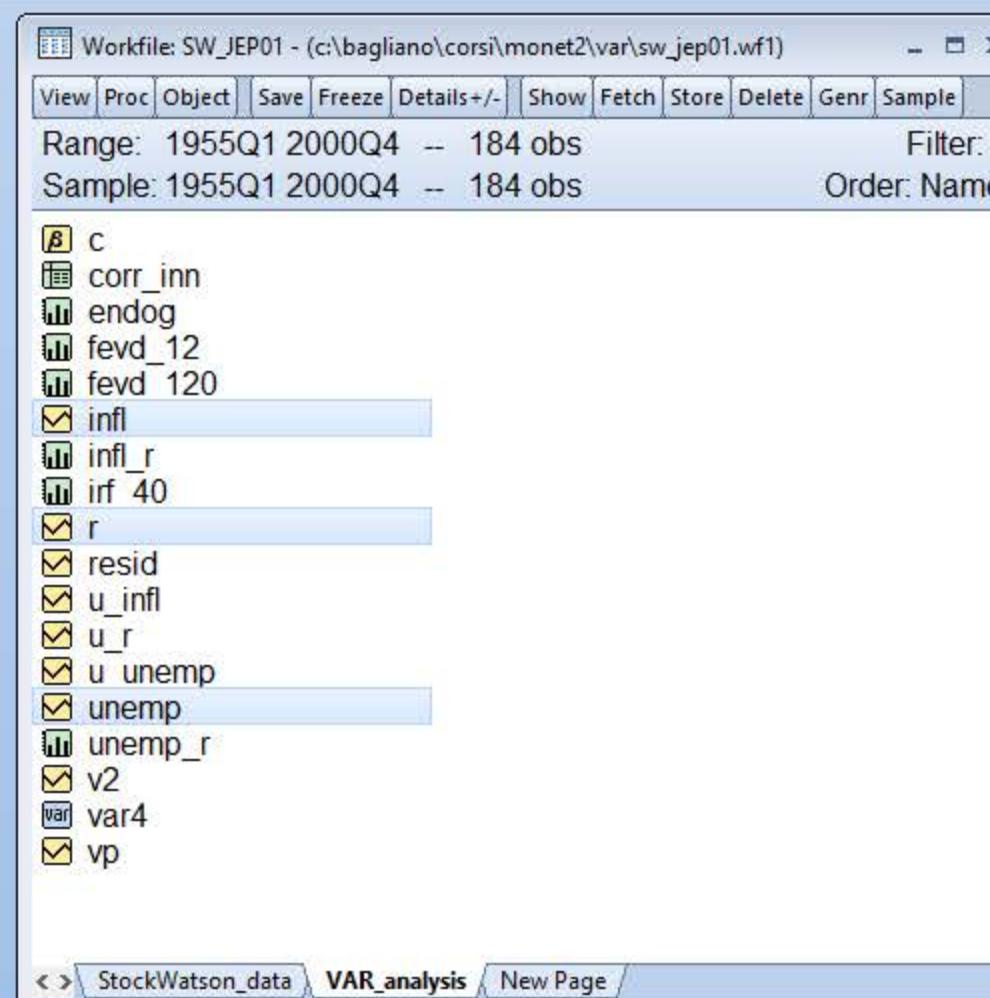
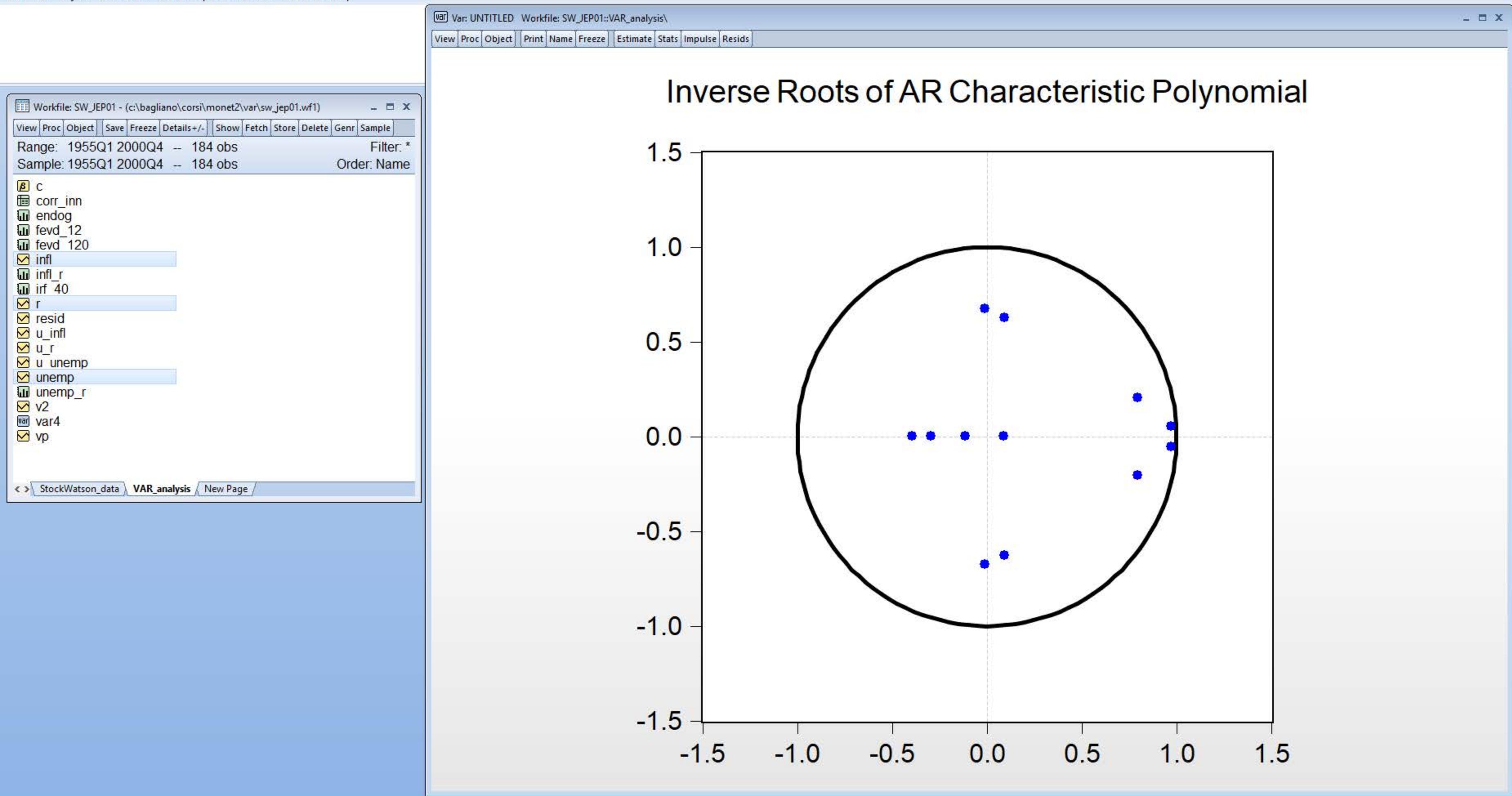
**Exogenous variables: C**

**Lag specification: 1 4**

**Date: 09/13/22 Time: 14:36**

| Root                  | Modulus  |
|-----------------------|----------|
| 0.971483 - 0.054282i  | 0.972998 |
| 0.971483 + 0.054282i  | 0.972998 |
| 0.795321 - 0.206719i  | 0.821747 |
| 0.795321 + 0.206719i  | 0.821747 |
| -0.010101 - 0.674997i | 0.675072 |
| -0.010101 + 0.674997i | 0.675072 |
| 0.091585 - 0.628600i  | 0.635237 |
| 0.091585 + 0.628600i  | 0.635237 |
| -0.395485             | 0.395485 |
| -0.296342             | 0.296342 |
| -0.115289             | 0.115289 |
| 0.090175              | 0.090175 |

**No root lies outside the unit circle.**  
**VAR satisfies the stability condition.**



Workfile: SW\_JEP01 - (c:\baglano\corsi\monet2\var\sw\_jep01.wf1)

View Proc Object Save Freeze Details+/- Show Fetch Store Delete Genr Sample

Range: 1955Q1 2000Q4 -- 184 obs Filter: \*

Sample: 1955Q1 2000Q4 -- 184 obs Order: Name

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- corr\_inn
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- irf\_40
- r
- resid
- u\_infl
- u\_r
- u\_unemp
- unemp
- unemp\_r
- v2
- var4
- vp

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[var] Var: UNTITLED Workfile: SW\_JEP01::VAR\_analysis

View Proc Object Print Name Freeze Estimate Stats Impulse Resids

### VAR Residual Serial Correlation L...

Null Hypothesis: no serial correlation

Date: 09/13/22 Time: 14:40

Sample: 1960Q1 2000Q4

Included observations: 164

| Lags | LM-Stat  | Prob   |
|------|----------|--------|
| 1    | 15.16624 | 0.0865 |
| 2    | 5.522029 | 0.7866 |
| 3    | 23.83104 | 0.0046 |
| 4    | 15.27946 | 0.0835 |
| 5    | 20.37984 | 0.0157 |
| 6    | 11.28607 | 0.2566 |
| 7    | 24.87633 | 0.0031 |
| 8    | 17.59728 | 0.0401 |

Probs from chi-square with 9 df.

Workfile: SW\_JEP01 - (c:\baglano\corsi\monet2\var\sw\_jep01.wf1)

View Proc Object Save Freeze Details+/- Show Fetch Store Delete Genr Sample

Range: 1955Q1 2000Q4 -- 184 obs Filter: \*

Sample: 1955Q1 2000Q4 -- 184 obs Order: Name

c  
corr\_inn  
endog  
fevd\_12  
fevd\_120  
infl  
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irf\_40  
r  
resid  
u\_infl  
u\_r  
u\_unemp  
unemp  
unemp\_r  
v2  
var4  
vp

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Var: UNTITLED Workfile: SW\_JEP01::VAR\_analysis

View Proc Object Print Name Freeze Estimate Stats Impulse Resids

Representations  
Estimation Output  
Residuals  
Endogenous Table  
Endogenous Graph  
Lag Structure  
Residual Tests  
Cointegration Test...  
Impulse Response...  
Variance Decomposition...  
Label

Serial Correlation L...  
is: no serial correlati...  
Time: 14:40

AR Roots Table  
AR Roots Graph  
Granger Causality/Block Exogeneity Tests  
Lag Exclusion Tests  
Lag Length Criteria...

|   | 15.16624 | 0.0865 |
|---|----------|--------|
| 1 | 15.16624 | 0.0865 |
| 2 | 5.522029 | 0.7866 |
| 3 | 23.83104 | 0.0046 |
| 4 | 15.27946 | 0.0835 |
| 5 | 20.37984 | 0.0157 |
| 6 | 11.28607 | 0.2566 |
| 7 | 24.87633 | 0.0031 |
| 8 | 17.59728 | 0.0401 |

Probs from chi-square with 9 df.

**VAR Lag Order Selection Criteria****Endogenous variables:** INFL UNEMP R**Exogenous variables:** C**Date:** 09/13/22 **Time:** 14:41**Sample:** 1960Q1 2000Q4**Included observations:** 164

| Lag | LogL      | LR        | FPE       | AIC       | SC        | HQ        |
|-----|-----------|-----------|-----------|-----------|-----------|-----------|
| 0   | -1046.961 | NA        | 73.02247  | 12.80440  | 12.86110  | 12.82742  |
| 1   | -478.0257 | 1110.117  | 0.079050  | 5.975923  | 6.202742  | 6.068003  |
| 2   | -430.6936 | 90.62371  | 0.049538  | 5.508458  | 5.905392* | 5.669598  |
| 3   | -411.4638 | 36.11438  | 0.043741  | 5.383705  | 5.950754  | 5.613906* |
| 4   | -400.7679 | 19.69622  | 0.042869  | 5.363023  | 6.100186  | 5.662283  |
| 5   | -395.7882 | 8.987612  | 0.045062  | 5.412052  | 6.319330  | 5.780372  |
| 6   | -378.4345 | 30.68647* | 0.040749* | 5.310177* | 6.387570  | 5.747558  |

\* indicates lag order selected by the criterion

LR: sequential modified LR test statistic (each test at 5% level)

FPE: Final prediction error

AIC: Akaike information criterion

SC: Schwarz information criterion

HQ: Hannan-Quinn information criterion

Table 1

**VAR Descriptive Statistics for ( $\pi$ ,  $u$ ,  $R$ )**


---

| <i>Regressor</i> | <i>Dependent Variable in Regression</i> |      |      |
|------------------|---|------|------|
|                  | $\pi$                                   | $u$  | $R$  |
| $\pi$            | 0.00                                    | 0.31 | 0.00 |
| $u$              | 0.02                                    | 0.00 | 0.00 |
| $R$              | 0.27                                    | 0.01 | 0.00 |

---

Var: UNTITLED Workfile: SW\_JEP01::VAR\_analysis\

View Proc Object Print Name Freeze Estimate Stats Impulse Resids

Representations  
Estimation Output  
Residuals  
Endogenous Table  
Endogenous Graph  
Lag Structure  
Residual Tests  
Cointegration Test...  
Impulse Response...  
Variance Decomposition...  
Label

Vector Autoregression Estimates  
Time: 14:35  
Q1 2000Q4

in [ ]

|           | INFL                                | UNEMP                                | R                                    |
|-----------|-------------------------------------|--------------------------------------|--------------------------------------|
| INFL(-1)  | 0.546602<br>(0.07866)<br>[ 6.94890] | 0.030733<br>(0.01870)<br>[ 1.64377]  | 0.086682<br>(0.06935)<br>[ 1.24984]  |
| INFL(-2)  | 0.075629<br>(0.08941)<br>[ 0.84583] | -0.030821<br>(0.02125)<br>[-1.45026] | 0.193629<br>(0.07884)<br>[ 2.45610]  |
| INFL(-3)  | 0.111728<br>(0.09006)<br>[ 1.24052] | 0.029789<br>(0.02141)<br>[ 1.39157]  | -0.078252<br>(0.07941)<br>[-0.98541] |
| INFL(-4)  | 0.266606<br>(0.08228)<br>[ 3.24007] | -0.024084<br>(0.01956)<br>[-1.23145] | -0.027216<br>(0.07255)<br>[-0.37514] |
| UNEMP(-1) | -0.938366                           | 1.484507                             | -1.565494                            |

Var: UNTITLED Workfile: SW\_JEP01::VAR\_analysis\

View Proc Object Print Name Freeze Estimate Stats Impulse Resids

## VAR Granger Causality/Block Exogeneity Wald Tests

Date: 09/13/22 Time: 15:16

Sample: 1960Q1 2000Q4

Included observations: 164

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Dependent variable: INFL

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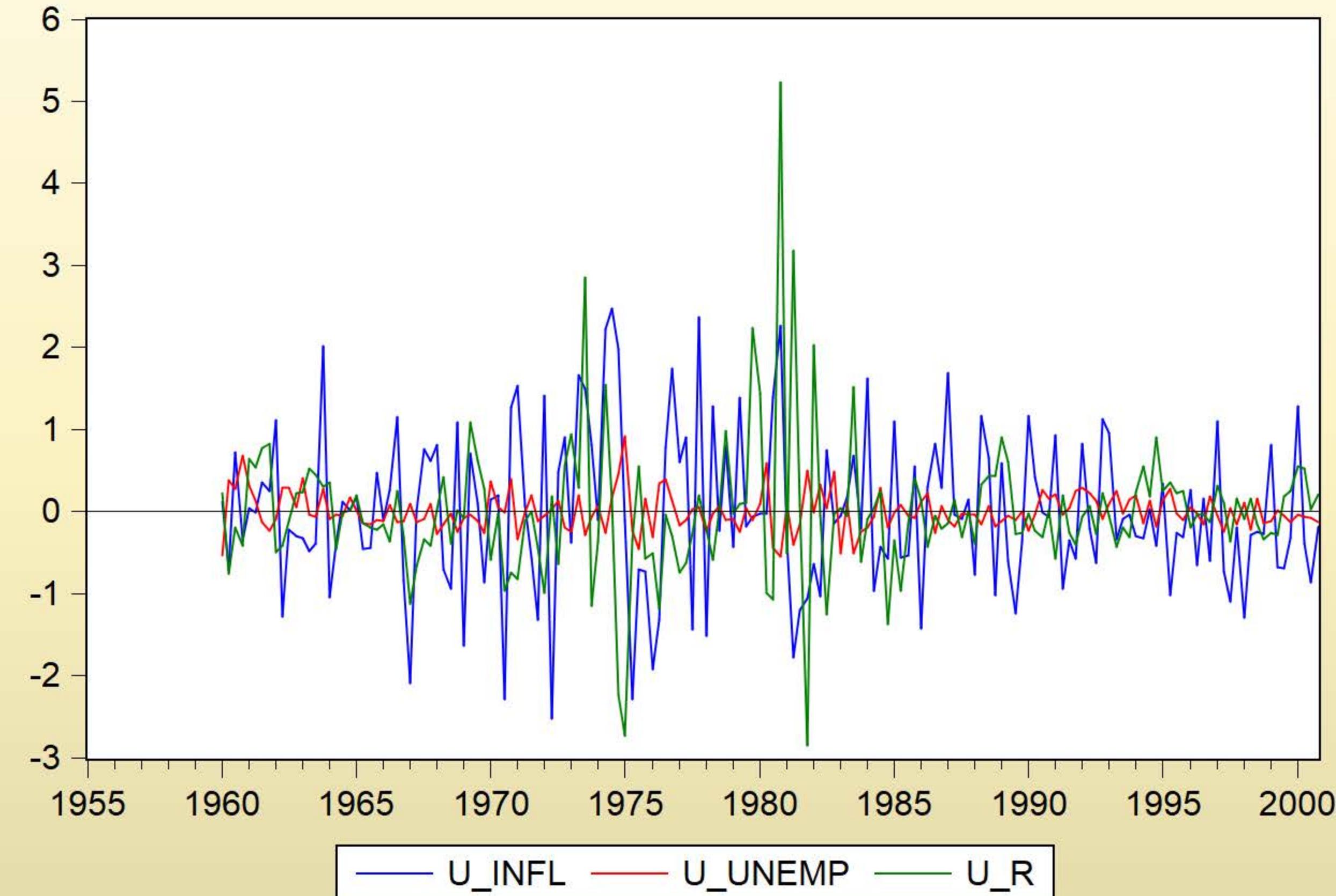
| Excluded | Chi-sq   | df | Prob.  |
|----------|----------|----|--------|
| UNEMP    | 12.40875 | 4  | 0.0146 |
| R        | 5.271804 | 4  | 0.2605 |
| All      | 33.22024 | 8  | 0.0001 |

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Dependent variable: UNEMP

---

| Excluded | Chi-sq   | df | Prob.  |
|----------|----------|----|--------|
| INFL     | 4.937588 | 4  | 0.2938 |
| R        | 14.59963 | 4  | 0.0056 |
| All      | 36.22794 | 8  | 0.0000 |



G Group: UNTITLED Workfile: SW\_JEP01::VAR\_analysis\

View Proc Object Print Name Freeze Sample Sheet Stats Spec

Workfile: SW\_JEP01 - (c:\bagliano\corsi\monet2\var\sw\_jep01.wf1)

View Proc Object Save Freeze Details+/- Show Fetch Store Delete

Range: 1955Q1 2000Q4 -- 184 obs  
Sample: 1955Q1 2000Q4 -- 184 obs

c  
corr\_inn  
endog  
fevd\_12  
fevd\_120  
infl  
infl\_r  
irf\_40  
r  
resid  
u\_infl  
u\_r  
u\_unemp  
unemp  
unemp\_r  
v2  
var4  
vp

Covariance Analysis: Ordinary  
Date: 09/13/22 Time: 15:35  
Sample (adjusted): 1960Q1 2000Q4  
Included observations: 164 after adjustments

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**Covariance**

|         | U_INFL                                       | U_UNEMP                                      | U_R                           |
|---------|--|--|-------------------------------|
| U_INFL  | 0.915067<br>1.000000<br>-----                |  |                               |
| U_UNEMP | -0.012144<br>-0.055836<br>-0.711782<br>----- | 0.051696<br>1.000000<br>-----                |                               |
| U_R     | 0.104424<br>0.129428<br>1.661322<br>-----    | -0.084804<br>-0.442225<br>-6.275599<br>----- | 0.711360<br>1.000000<br>----- |

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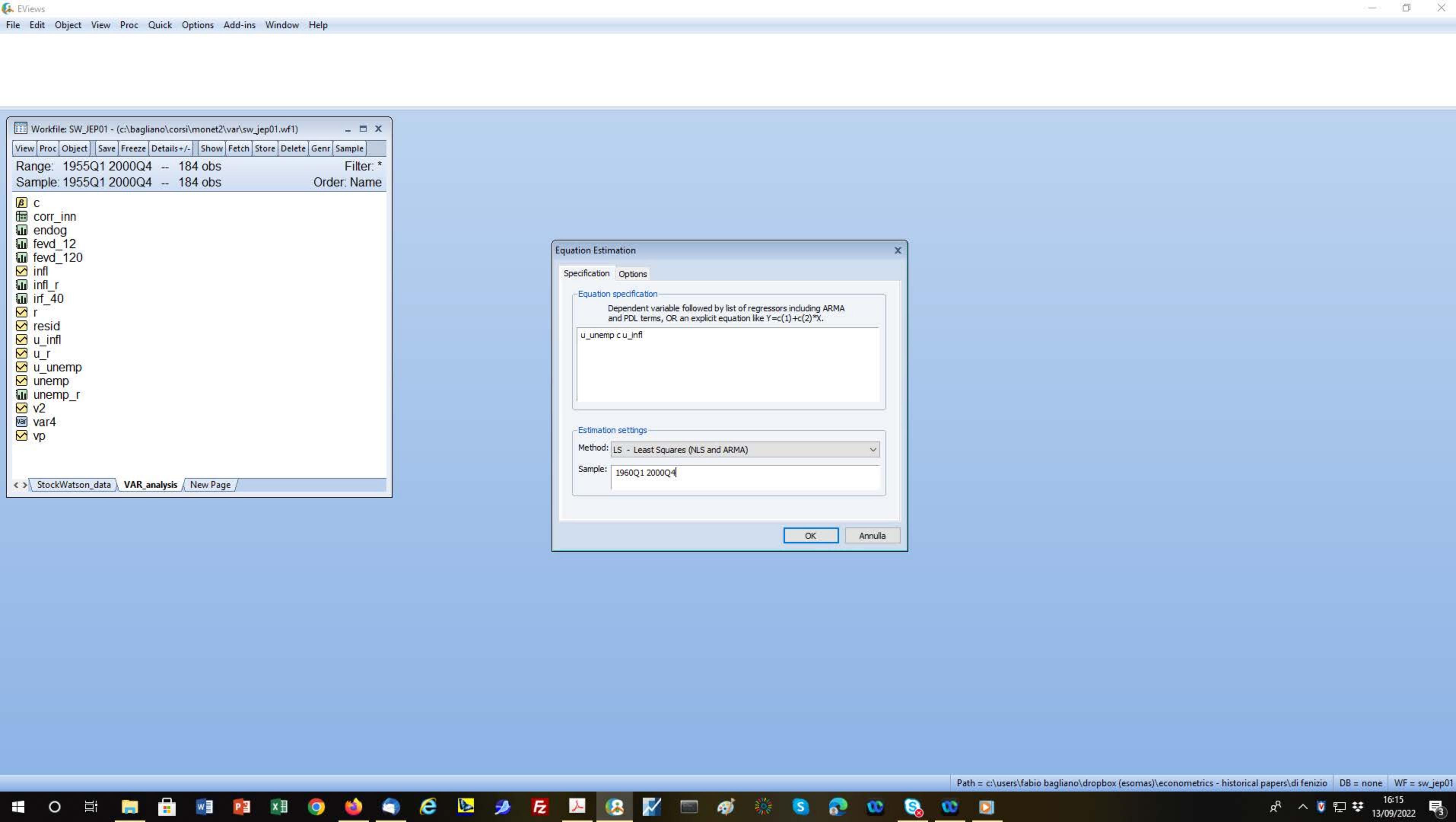
Relation between VAR innovations and structural disturbances  
based on a Choleski (recursive) identification scheme:

$$\begin{pmatrix} 1 & 0 & 0 \\ a_{21} & 1 & 0 \\ a_{31} & a_{32} & 1 \end{pmatrix} \begin{pmatrix} u_t^\pi \\ u_t^U \\ u_t^R \end{pmatrix} = \begin{pmatrix} v_t^1 \\ v_t^2 \\ v_t^P \end{pmatrix}$$

$$u_t^\pi = v_t^1$$

$$\Rightarrow u_t^U = -a_{21}u_t^\pi + v_t^2$$

$$u_t^R = -a_{31}u_t^\pi - a_{32}u_t^U + v_t^P$$



Workfile: SW\_JEP01 - (c:\bagliano\corsi\monet2\var\sw\_jep01.wf1) - □ X

View Proc Object Save Freeze Details+/- Show Fetch Store Delete Genr Sample

Range: 1955Q1 2000Q4 -- 184 obs Filter: \*

Sample: 1955Q1 2000Q4 -- 184 obs Order: Name

c  
 corr\_inn  
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 v2  
 var4  
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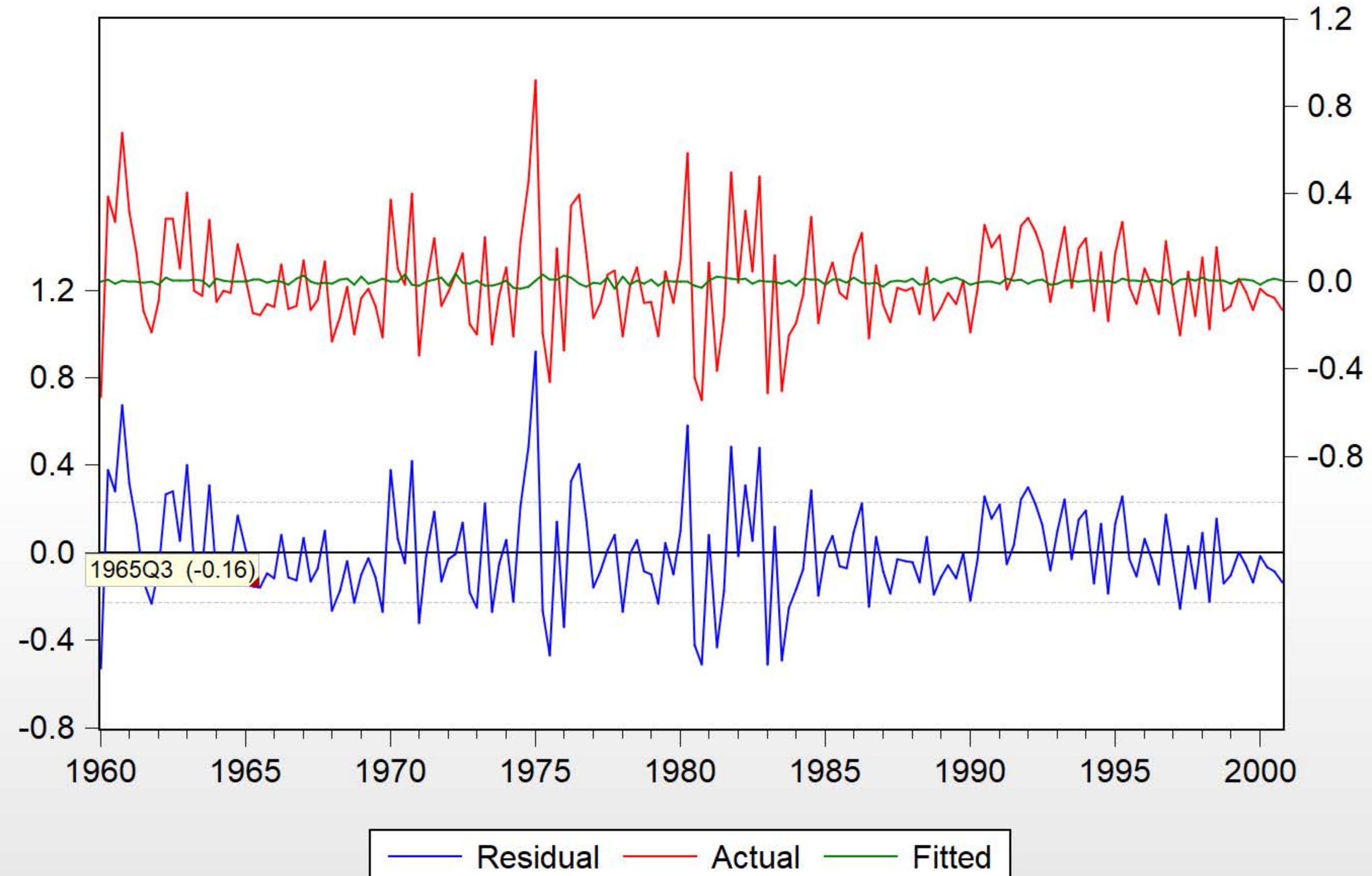
Equation: UNTITLED Workfile: SW\_JEP01::VAR\_analysis - □ X

View Proc Object Print Name Freeze Estimate Forecast Stats Resids

**Dependent Variable: U\_UNEMP**  
**Method: Least Squares**  
**Date: 09/13/22 Time: 16:15**  
**Sample: 1960Q1 2000Q4**  
**Included observations: 164**

| Variable | Coefficient | Std. Error | t-Statistic | Prob.  |
|----------|-------------|------------|-------------|--------|
| C        | -1.10E-15   | 0.017836   | -6.14E-14   | 1.0000 |
| U_INFL   | -0.013271   | 0.018645   | -0.711782   | 0.4776 |

|                    |           |                       |           |
|--------------------|-----------|-----------------------|-----------|
| R-squared          | 0.003118  | Mean dependent var    | -1.10E-15 |
| Adjusted R-squared | -0.003036 | S.D. dependent var    | 0.228064  |
| S.E. of regression | 0.228410  | Akaike info criterion | -0.103229 |
| Sum squared resid  | 8.451722  | Schwarz criterion     | -0.065426 |
| Log likelihood     | 10.46477  | Hannan-Quinn criter.  | -0.087882 |
| F-statistic        | 0.506634  | Durbin-Watson stat    | 1.898031  |
| Prob(F-statistic)  | 0.477623  |                       |           |



Workfile: SW\_JEP01 - (c:\bagliano\corsi\monet2\var\sw\_jep01.wf1) - □ X

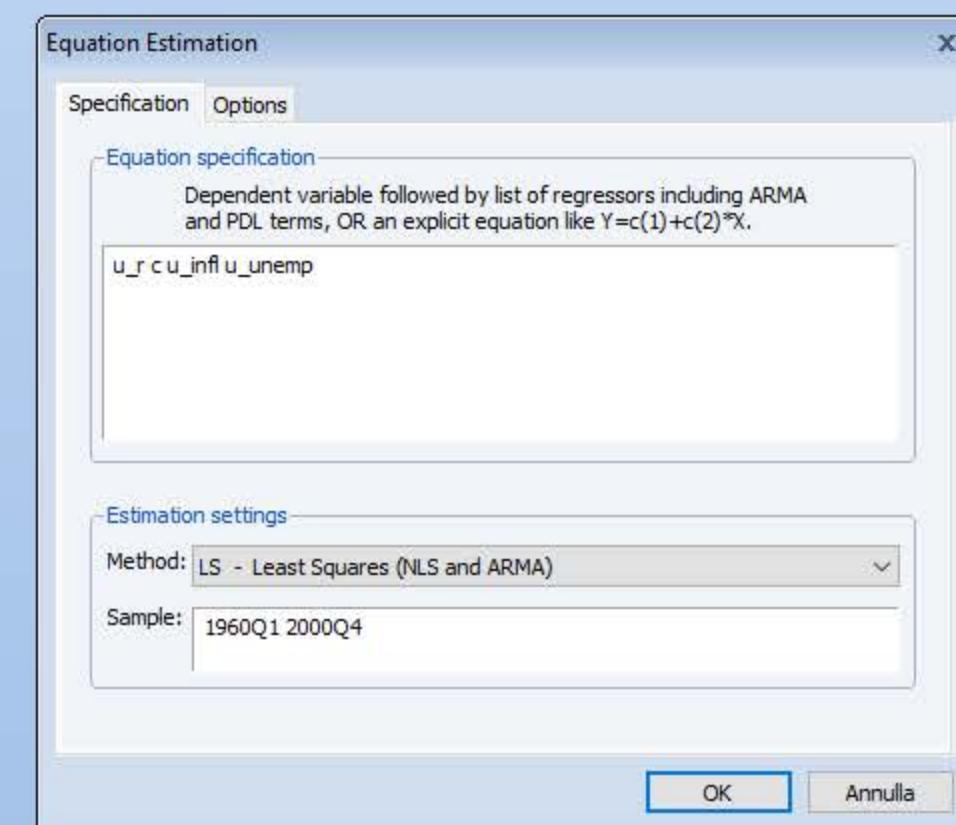
View Proc Object Save Freeze Details+/- Show Fetch Store Delete Genr Sample

Range: 1955Q1 2000Q4 -- 184 obs Filter: \*

Sample: 1955Q1 2000Q4 -- 184 obs Order: Name

c  
 corr\_inn  
 endog  
 fevd\_12  
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 u\_infl  
 u\_r  
 u\_unemp  
 unemp  
 unemp\_r  
 v2  
 var4  
 vp

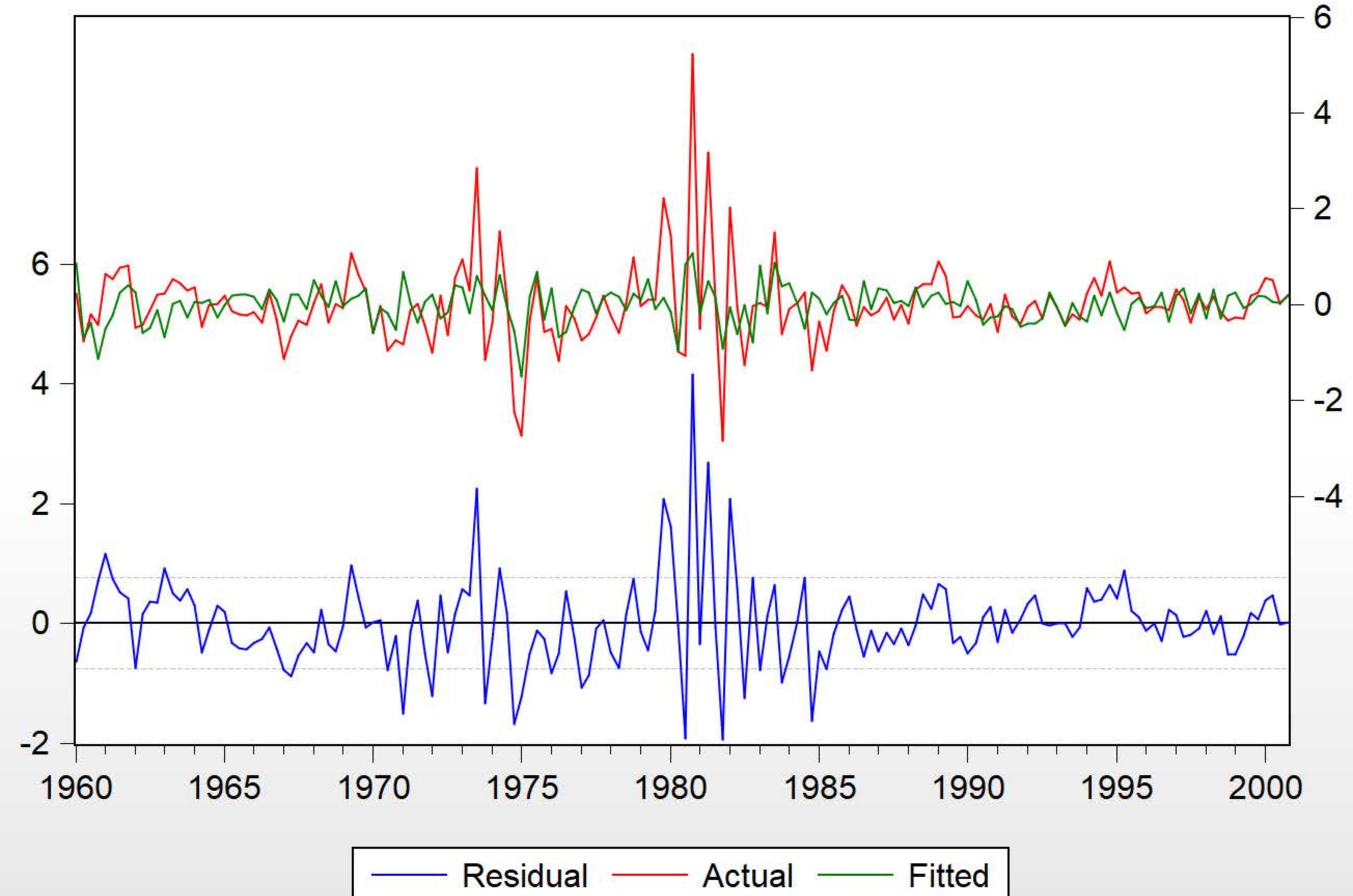
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| Workfile: SW_JEP01 - (c:\bagliano\corsi\monet2\var\sw_jep01.wf1) |             |
|--|-------------|
|  |             |
| View   | Proc        |
| Object   | Save        |
| Freeze   | Details +/- |
| Show   | Fetch       |
| Store  | Delete      |
| Genr   | Sample      |
| Range: 1955Q1 2000Q4 -- 184 obs                                  | Filter: *   |
| Sample: 1955Q1 2000Q4 -- 184 obs                                 | Order: Name |
| <input checked="" type="checkbox"/> c                            |             |
| <input type="checkbox"/> corr_inn                                |             |
| <input type="checkbox"/> endog                                   |             |
| <input type="checkbox"/> fevd_12                                 |             |
| <input type="checkbox"/> fevd_120                                |             |
| <input checked="" type="checkbox"/> infl                         |             |
| <input type="checkbox"/> infl_r                                  |             |
| <input type="checkbox"/> irf_40                                  |             |
| <input checked="" type="checkbox"/> r                            |             |
| <input checked="" type="checkbox"/> resid                        |             |
| <input checked="" type="checkbox"/> u_infl                       |             |
| <input checked="" type="checkbox"/> u_r                          |             |
| <input checked="" type="checkbox"/> u_unemp                      |             |
| <input checked="" type="checkbox"/> unemp                        |             |
| <input type="checkbox"/> unemp_r                                 |             |
| <input checked="" type="checkbox"/> v2                           |             |
| <input type="checkbox"/> var4                                    |             |
| <input checked="" type="checkbox"/> vp                           |             |

< > StockWatson\_data VAR\_analysis New Page

| Equation: UNTITLED Workfile: SW_JEP01::VAR_analysis\ |             |                       |             |        |
|--|-------------|-----------------------|-------------|--------|
| View   | Proc        | Object                | Print       | Name   |
|  |             |                       | Freeze      |        |
|  |             |                       | Estimate    |        |
|  |             |                       | Forecast    |        |
|  |             |                       | Stats       |        |
|  |             |                       | Resids      |        |
| <b>Dependent Variable: U_R</b>                       |             |                       |             |        |
| <b>Method: Least Squares</b>                         |             |                       |             |        |
| <b>Date: 09/13/22 Time: 16:17</b>                    |             |                       |             |        |
| <b>Sample: 1960Q1 2000Q4</b>                         |             |                       |             |        |
| <b>Included observations: 164</b>                    |             |                       |             |        |
| Variable   | Coefficient | Std. Error            | t-Statistic | Prob.  |
| C  | 2.69E-15    | 0.059209              | 4.54E-14    | 1.0000 |
| U_INFL   | 0.092634    | 0.061992              | 1.494279    | 0.1371 |
| U_UNEMP  | -1.618676   | 0.260817              | -6.206172   | 0.0000 |
| R-squared  | 0.206567    | Mean dependent var    | 4.52E-15    |        |
| Adjusted R-squared                                   | 0.196711    | S.D. dependent var    | 0.846005    |        |
| S.E. of regression                                   | 0.758243    | Akaike info criterion | 2.302499    |        |
| Sum squared resid                                    | 92.56423    | Schwarz criterion     | 2.359204    |        |
| Log likelihood                                       | -185.8049   | Hannan-Quinn criter.  | 2.325519    |        |
| F-statistic  | 20.95786    | Durbin-Watson stat    | 1.984411    |        |
| Prob(F-statistic)                                    | 0.000000    |                       |             |        |



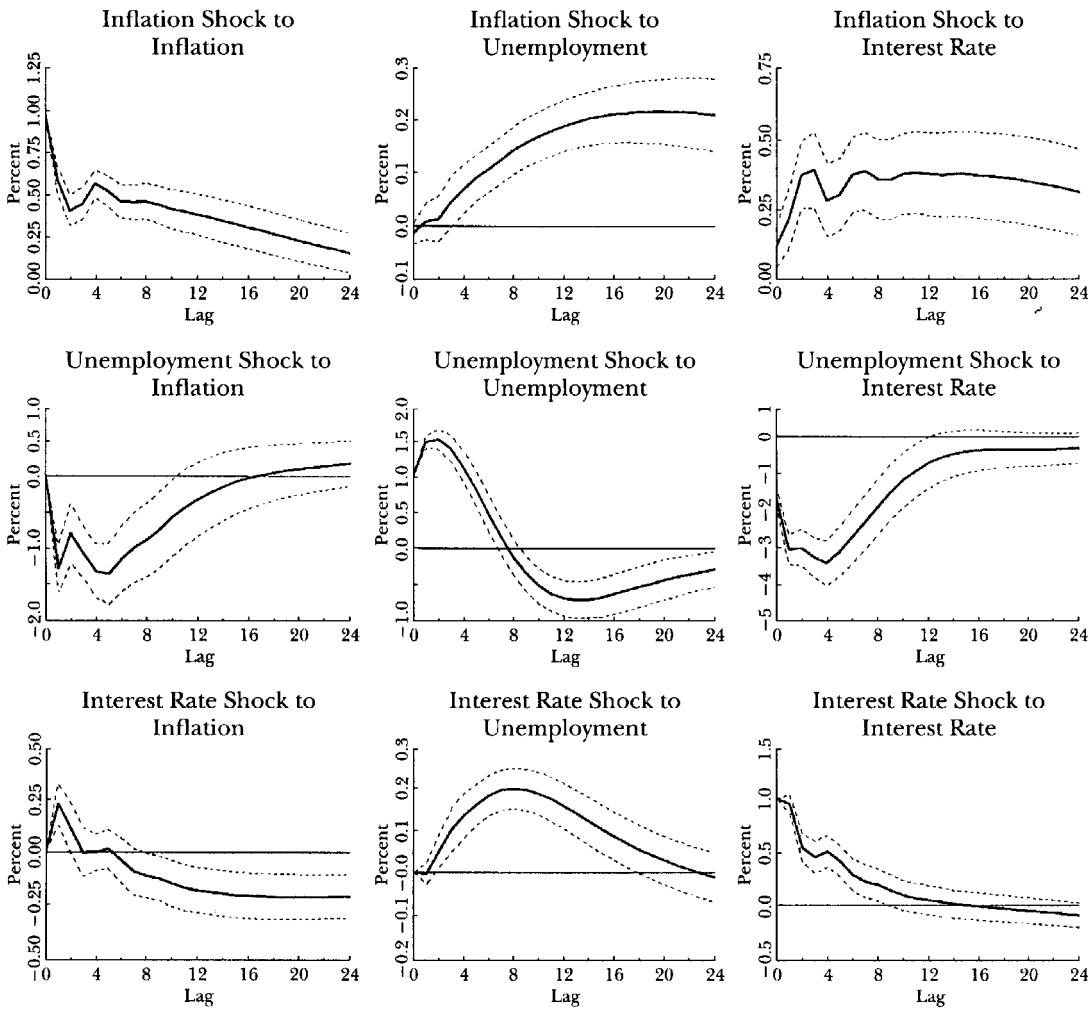
$$\begin{aligned}
u_t^\pi &= v_t^1 \\
\Rightarrow u_t^U &= -a_{21}u_t^\pi + v_t^2 \\
u_t^R &= -a_{31}u_t^\pi - a_{32}u_t^U + v_t^P
\end{aligned}$$

Inverting A:

$$\begin{aligned}
u_t^\pi &= v_t^1 \\
u_t^U &= -a_{21}v_t^1 + v_t^2 \\
u_t^R &= -(a_{31} - a_{32}a_{21})v_t^1 - a_{32}v_t^2 + v_t^P
\end{aligned}$$

Figure 1

# Impulse Responses in the Inflation-Unemployment-Interest Rate Recursive VAR



Workfile: SW\_JEP01 - (c:\baglano\corsi\monet2\var\sw\_jep01.wf1)

View Proc Object Save Freeze Details+/- Show Fetch Store Delete Genr Sample

Range: 1955Q1 2000Q4 -- 184 obs Filter: \*

Sample: 1955Q1 2000Q4 -- 184 obs Order: Name

- c
- corr\_inn
- endog
- fevd\_12
- fevd\_120
- infl
- infl\_r
- irf\_40
- r
- resid
- u\_infl
- u\_r
- u\_unemp
- unemp
- unemp\_r
- v2
- var4
- vp

< > StockWatson\_data VAR\_analysis New Page

Var: UNTITLED Workfile: SW\_JEP01::VAR\_analysis\

View Proc Object Print Name Freeze Estimate Stats Impulse Resids

Representations  
Estimation Output  
Residuals  
Endogenous Table  
Endogenous Graph  
Lag Structure  
Residual Tests  
Cointegration Test...  
**Impulse Response...**  
Variance Decomposition...  
Label

Vector Autoregression Estimates

Date: 2022-09-13 Time: 16:26

Sample: 1955Q1 2000Q4

Observations: 164

Coef. in ( ) & t-statistics in [ ]

|           | INFL                                | UNEMP                                | R                                    |
|-----------|-------------------------------------|--------------------------------------|--------------------------------------|
| INFL(-1)  | 0.546602<br>(0.07866)<br>[ 6.94890] | 0.030733<br>(0.01870)<br>[ 1.64377]  | 0.086682<br>(0.06935)<br>[ 1.24984]  |
| INFL(-2)  | 0.075629<br>(0.08941)<br>[ 0.84583] | -0.030821<br>(0.02125)<br>[-1.45026] | 0.193629<br>(0.07884)<br>[ 2.45610]  |
| INFL(-3)  | 0.111728<br>(0.09006)<br>[ 1.24052] | 0.029789<br>(0.02141)<br>[ 1.39157]  | -0.078252<br>(0.07941)<br>[-0.98541] |
| INFL(-4)  | 0.266606<br>(0.08228)<br>[ 3.24007] | -0.024084<br>(0.01956)<br>[-1.23145] | -0.027216<br>(0.07255)<br>[-0.37514] |
| UNEMP(-1) | -0.938366                           | 1.484507                             | -1.565494                            |

Workfile: SW\_JEP01 - (c:\bagliano\corsi\monet2\var\sw\_jep01.wf1)

View Proc Object Save Freeze Details+/- Show Fetch Store Delete Genr Sample

Range: 1955Q1 2000Q4 -- 184 obs Filter: \*

Sample: 1955Q1 2000Q4 -- 184 obs Order: Name

- c
- corr\_inn
- endog
- fevd\_12
- fevd\_120
- infl
- infl\_r
- irf\_40
- r
- resid
- u\_infl
- u\_r
- u\_unemp
- unemp
- unemp\_r
- v2
- var4
- vp

< > StockWatson\_data VAR\_analysis New Page

Var: UNTITLED Workfile: SW\_JEP01::VAR\_analysis\

View Proc Object Print Name Freeze Estimate Stats Impulse Resids

Vector Autoregression Estimates

**Vector Autoregression Estimates**  
**Date: 09/13/22 Time: 16:26**  
**Sample: 1960Q1 2000Q4**  
**Included observations: 164**  
**Standard errors in ( ) & t-statistics in [ ]**

|                  | INFL   | UNEMP   | R   |
|------------------|--|---|---|
| <b>INFL(-1)</b>  |  |   | <b>0.086682<br/>(0.06935)<br/>[ 1.24984]</b>  |
| <b>INFL(-2)</b>  |  |   | <b>0.193629<br/>(0.07884)<br/>[ 2.45610]</b>  |
| <b>INFL(-3)</b>  | <b>0.111728<br/>(0.09006)<br/>[ 1.24052]</b> | <b>0.029789<br/>(0.02141)<br/>[ 1.39157]</b>  | <b>-0.078252<br/>(0.07941)<br/>[-0.98541]</b> |
| <b>INFL(-4)</b>  | <b>0.266606<br/>(0.08228)<br/>[ 3.24007]</b> | <b>-0.024084<br/>(0.01956)<br/>[-1.23145]</b> | <b>-0.027216<br/>(0.07255)<br/>[-0.37514]</b> |
| <b>UNEMP(-1)</b> | <b>-0.938366</b>                             | <b>1.484507</b>                               | <b>-1.565494</b>                              |

Impulse Responses

Display Impulse Definition

Display Format:
 Table
 Multiple Graphs
 Combined Graphs

Display Information:
 Impulses:  
 infl unemp r

Response Standard Errors:
  None
  Analytic (asymptotic)
  Monte Carlo

Repetitions: 100

Periods: 40

Accumulated Responses

OK Annulla

Workfile: SW\_JEP01 - (c:\bagliano\corsi\monet2\var\sw\_jep01.wf1)

View Proc Object Save Freeze Details+/- Show Fetch Store Delete Genr Sample

Range: 1955Q1 2000Q4 -- 184 obs Filter: \*

Sample: 1955Q1 2000Q4 -- 184 obs Order: Name

- c
- corr\_inn
- endog
- fevd\_12
- fevd\_120
- infl
- infl\_r
- irf\_40
- r
- resid
- u\_infl
- u\_r
- u\_unemp
- unemp
- unemp\_r
- v2
- var4
- vp

< > StockWatson\_data VAR\_analysis New Page

Var: UNTITLED Workfile: SW\_JEP01::VAR\_analysis\

View Proc Object Print Name Freeze Estimate Stats Impulse Resids

Vector Autoregression Estimates

**Vector Autoregression Estimates**  
**Date: 09/13/22 Time: 16:26**  
**Sample: 1960Q1 2000Q4**  
**Included observations: 164**  
**Standard errors in ( ) & t-statistics in [ ]**

|                  | INFL                                | UNEMP                                | R                                    |
|------------------|-------------------------------------|--------------------------------------|--------------------------------------|
| <b>INFL(-1)</b>  |                                     |                                      |                                      |
| <b>INFL(-2)</b>  |                                     |                                      |                                      |
| <b>INFL(-3)</b>  | 0.111728<br>(0.09006)<br>[ 1.24052] | 0.029789<br>(0.02141)<br>[ 1.39157]  | -0.078252<br>(0.07941)<br>[-0.98541] |
| <b>INFL(-4)</b>  | 0.266606<br>(0.08228)<br>[ 3.24007] | -0.024084<br>(0.01956)<br>[-1.23145] | -0.027216<br>(0.07255)<br>[-0.37514] |
| <b>UNEMP(-1)</b> | -0.938366                           | 1.484507                             | -1.565494                            |

Impulse Responses

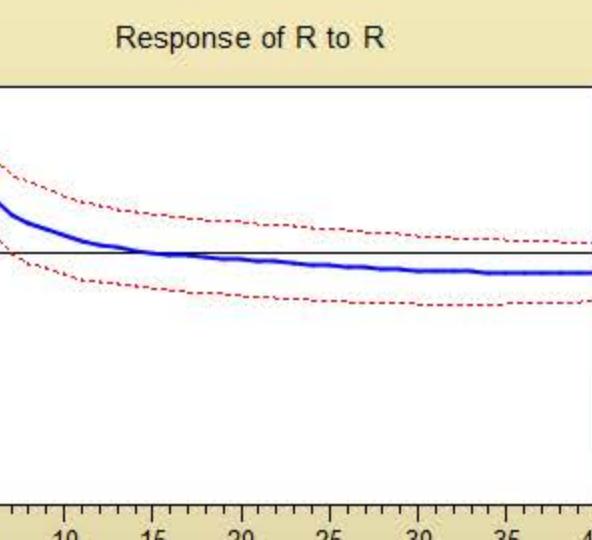
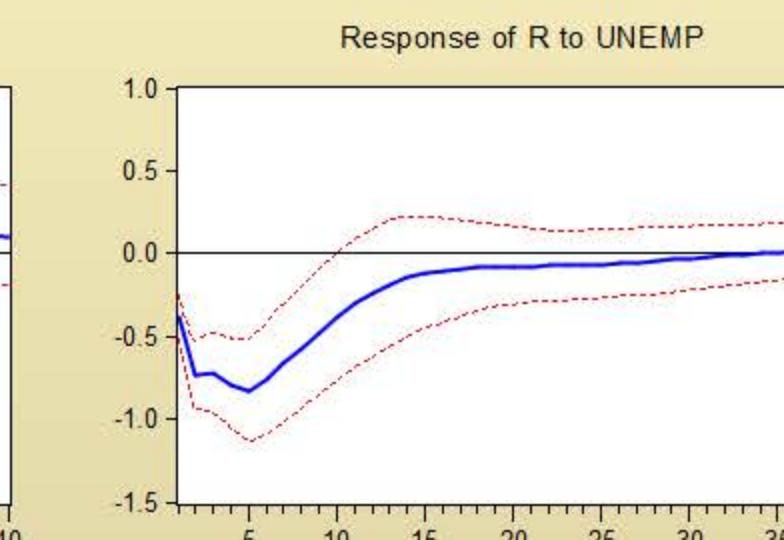
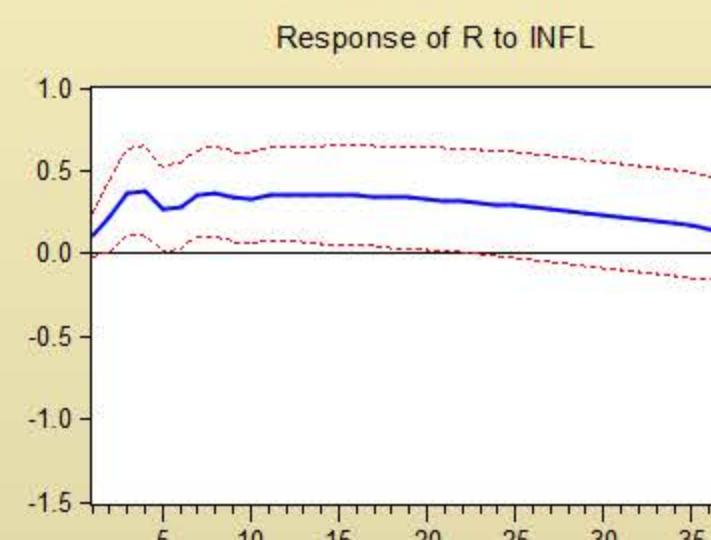
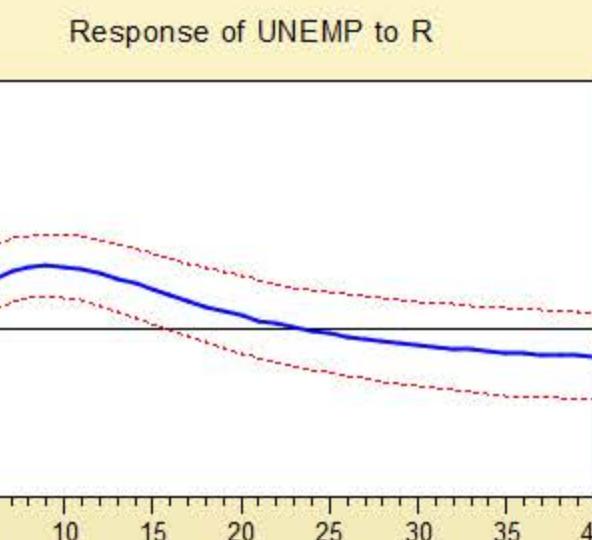
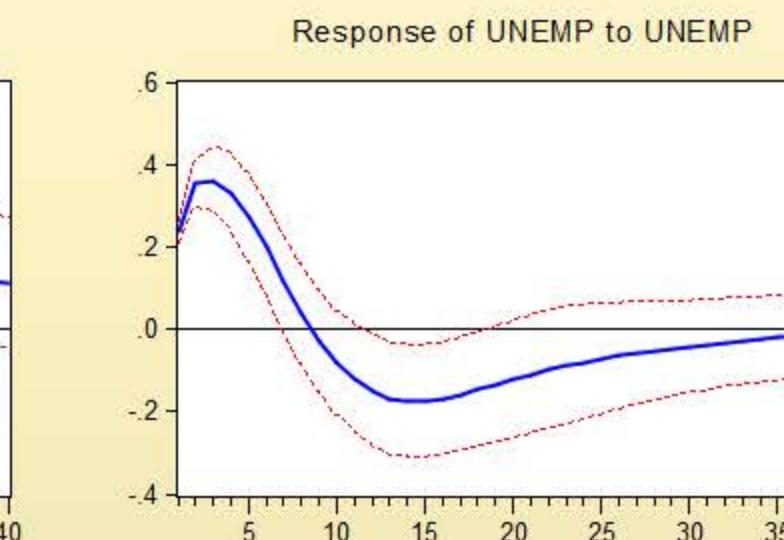
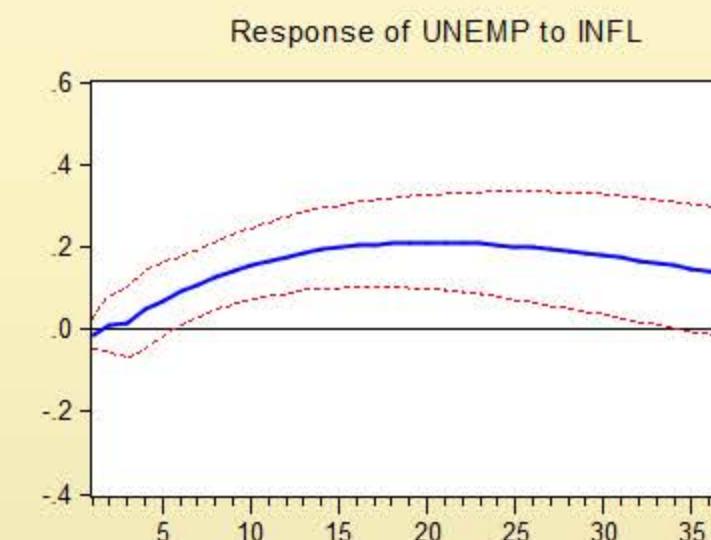
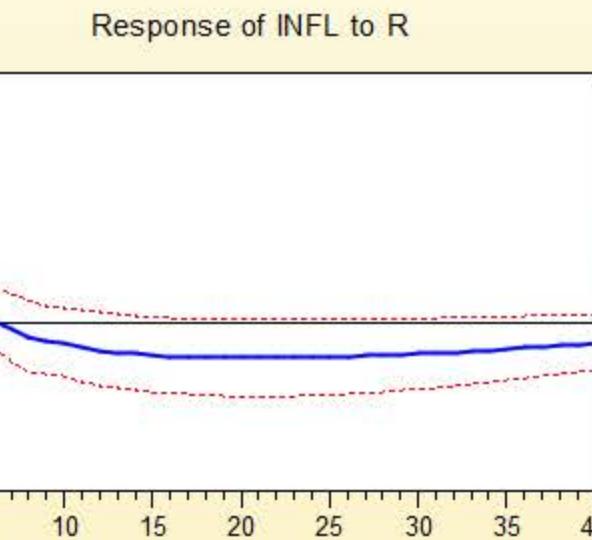
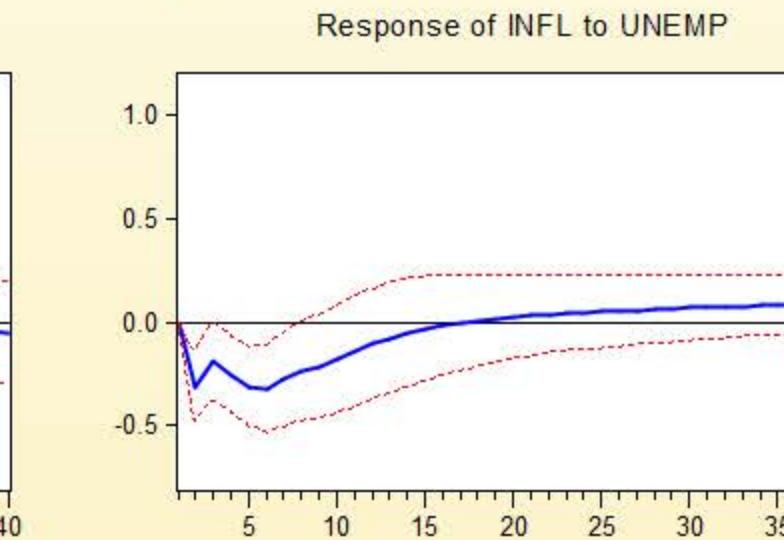
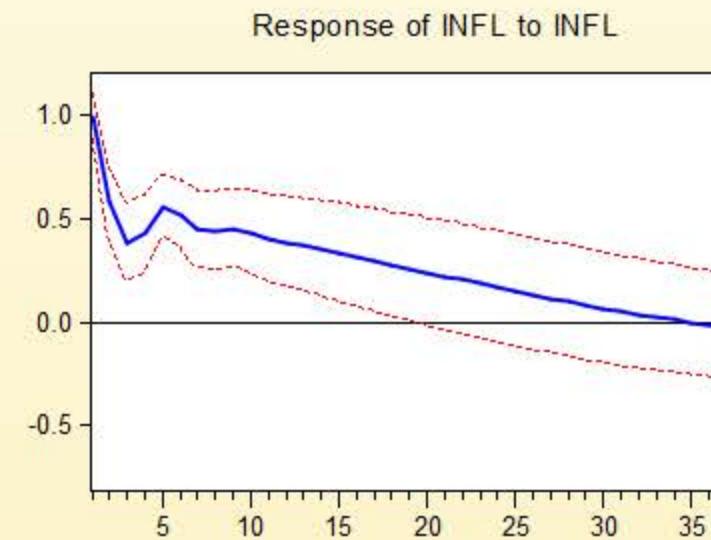
Display Impulse Definition

Decomposition Method:

- Residual - one unit
- Residual - one std.deviation
- Cholesky - dof adjusted
- Cholesky - no dof adjustment
- Generalized Impulses
- Structural Decomposition
- User Specified

Cholesky Ordering:  
infl unemp r

OK Annulla

Response to Cholesky One S.D. Innovations  $\pm 2$  S.E.

Workfile: SW\_JEP01 - (c:\baglano\corsi\monet2\var\sw\_jep01.wf1)

View Proc Object Save Freeze Details+/- Show Fetch Store Delete Genr Sample

Range: 1955Q1 2000Q4 -- 184 obs Filter: \*

Sample: 1955Q1 2000Q4 -- 184 obs Order: Name

- c
- corr\_inn
- endog
- fevd\_12
- fevd\_120
- infl
- infl\_r
- irf\_40
- r
- resid
- u\_infl
- u\_r
- u\_unemp
- unemp
- unemp\_r
- v2
- var4
- vp

< > StockWatson\_data VAR\_analysis New Page

Var: UNTITLED Workfile: SW\_JEP01::VAR\_analysis\

View Proc Object Print Name Freeze Estimate Stats Impulse Resids

Representations  
Estimation Output  
Residuals  
Endogenous Table  
Endogenous Graph  
Lag Structure  
Residual Tests  
Cointegration Test...  
Impulse Response...  
Variance Decomposition...  
Label

Vector Autoregression Estimates

Date: 22/09/2022 Time: 16:26

Sample: 1955Q1 2000Q4

Observations: 164

Dependent variables in ( ) & t-statistics in [ ]

|           | INFL                                | UNEMP                                | R                                    |
|-----------|-------------------------------------|--------------------------------------|--------------------------------------|
| INFL(-1)  | 0.546602<br>(0.07866)<br>[ 6.94890] | 0.030733<br>(0.01870)<br>[ 1.64377]  | 0.086682<br>(0.06935)<br>[ 1.24984]  |
| INFL(-2)  | 0.075629<br>(0.08941)<br>[ 0.84583] | -0.030821<br>(0.02125)<br>[-1.45026] | 0.193629<br>(0.07884)<br>[ 2.45610]  |
| INFL(-3)  | 0.111728<br>(0.09006)<br>[ 1.24052] | 0.029789<br>(0.02141)<br>[ 1.39157]  | -0.078252<br>(0.07941)<br>[-0.98541] |
| INFL(-4)  | 0.266606<br>(0.08228)<br>[ 3.24007] | -0.024084<br>(0.01956)<br>[-1.23145] | -0.027216<br>(0.07255)<br>[-0.37514] |
| UNEMP(-1) | -0.938366                           | 1.484507                             | -1.565494                            |

Workfile: SW\_JEP01 - (c:\bagliano\corsi\monet2\var\sw\_jep01.wf1)

View Proc Object Save Freeze Details+/- Show Fetch Store Delete Genr Sample

Range: 1955Q1 2000Q4 -- 184 obs Filter: \*

Sample: 1955Q1 2000Q4 -- 184 obs Order: Name

c  
 corr\_inn  
 endog  
 fevd\_12  
 fevd\_120  
 infl  
 infl\_r  
 irf\_40  
 r  
 resid  
 u\_infl  
 u\_r  
 u\_unemp  
 unemp  
 unemp\_r  
 v2  
 var4  
 vp

< > StockWatson\_data VAR\_analysis New Page

Var: UNTITLED Workfile: SW\_JEP01::VAR\_analysis\

View Proc Object Print Name Freeze Estimate Stats Impulse Resids

Vector Autoregression Estimates

**Vector Autoregression Estimates**  
**Date: 09/13/22 Time: 16:26**  
**Sample: 1960Q1 2000Q4**  
**Included observations: 164**  
**Standard errors in ( ) & t-statistics in [ ]**

**INFL**

**INFL**

**INFL(-3)**

**INFL(-4)**

**UNEMP(-1)**

**UNEMP** **R**

|                 | <b>UNEMP</b>  | <b>R</b>  |
|-----------------|---|---|
| <b>INFL</b>     | <b>0.030733</b><br><b>(0.01870)</b><br><b>[ 1.64377]</b>  | <b>0.086682</b><br><b>(0.06935)</b><br><b>[ 1.24984]</b>  |
| <b>INFL(-3)</b> | <b>-0.030821</b><br><b>(0.02125)</b><br><b>[-1.45026]</b> | <b>0.193629</b><br><b>(0.07884)</b><br><b>[ 2.45610]</b>  |
| <b>INFL(-4)</b> | <b>0.111728</b><br><b>(0.09006)</b><br><b>[ 1.24052]</b>  | <b>0.029789</b><br><b>(0.02141)</b><br><b>[ 1.39157]</b>  |
|                 | <b>0.266606</b><br><b>(0.08228)</b><br><b>[ 3.24007]</b>  | <b>-0.024084</b><br><b>(0.01956)</b><br><b>[-1.23145]</b> |
|                 | <b>-0.938366</b>  | <b>1.484507</b>   |
|                 |   | <b>-1.565494</b>  |

VAR Variance Decompositions

Display Format:  Combined Graphs  
 Table  
 Multiple Graphs

Display Information: Decompositions of: infl unemp r  
Periods: 12

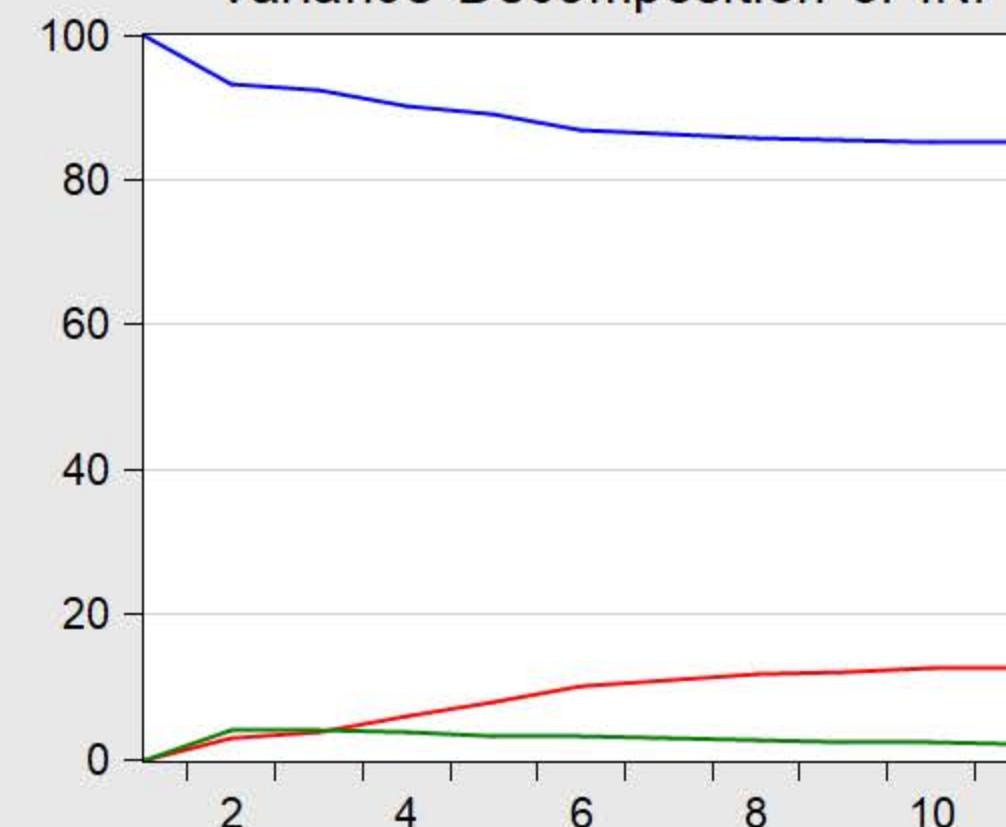
Standard Errors: None  
 Monte Carlo

Factorization: Cholesky Decomposition  
 Structural Decomposition

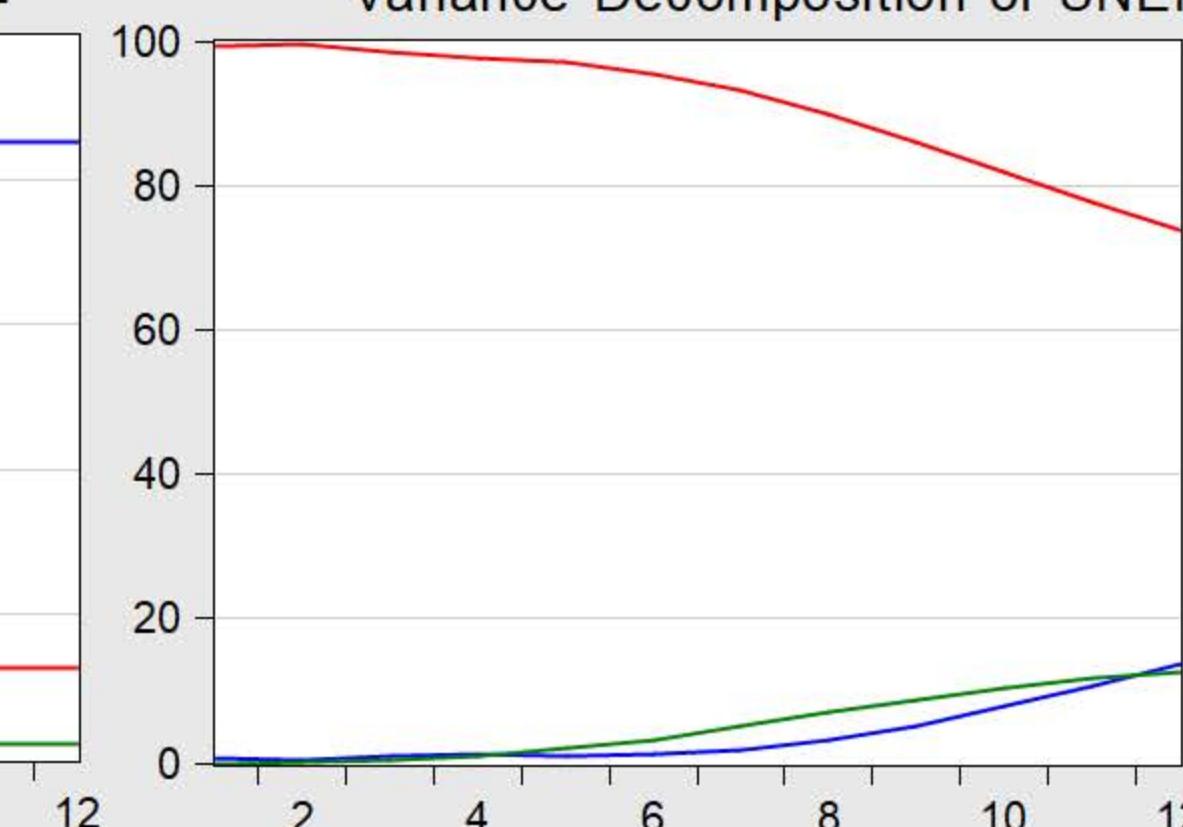
Ordering for Cholesky: infl unemp r  
Repetitions for Monte Carlo: 100

OK Cancel

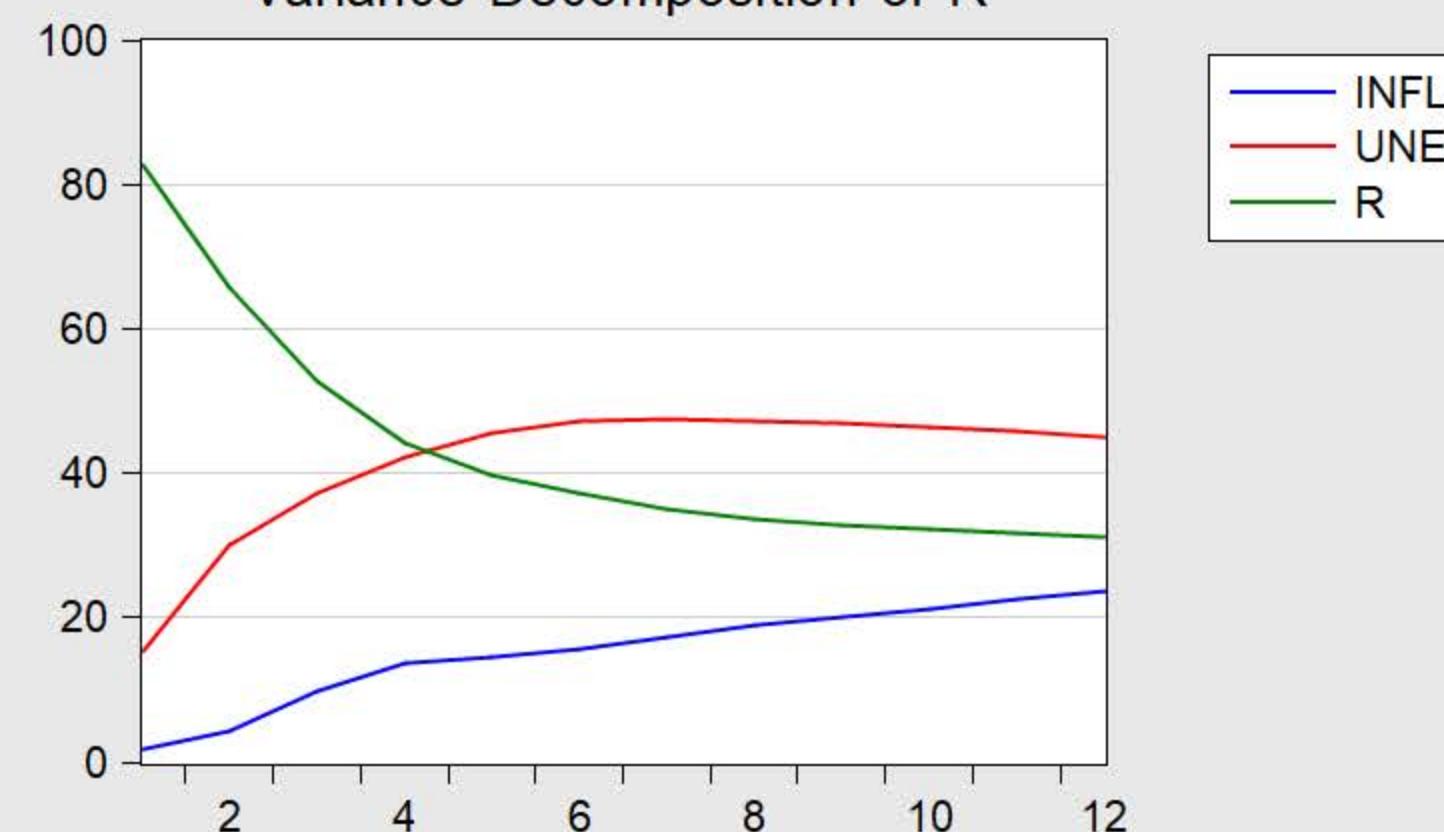
Variance Decomposition of INFL



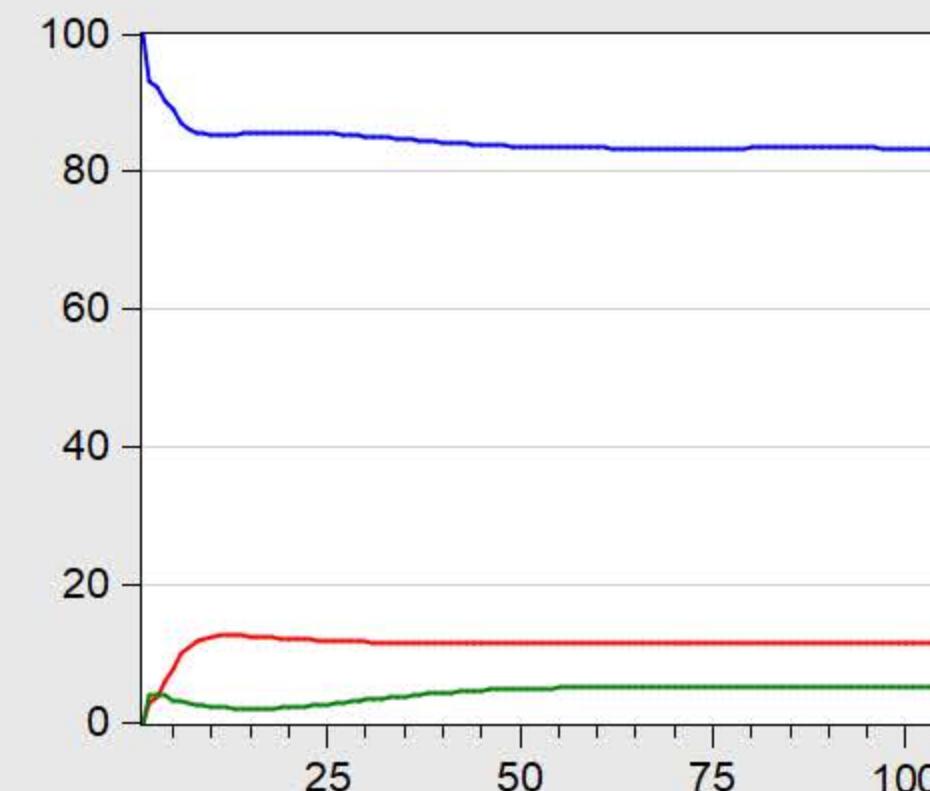
Variance Decomposition of UNEMP



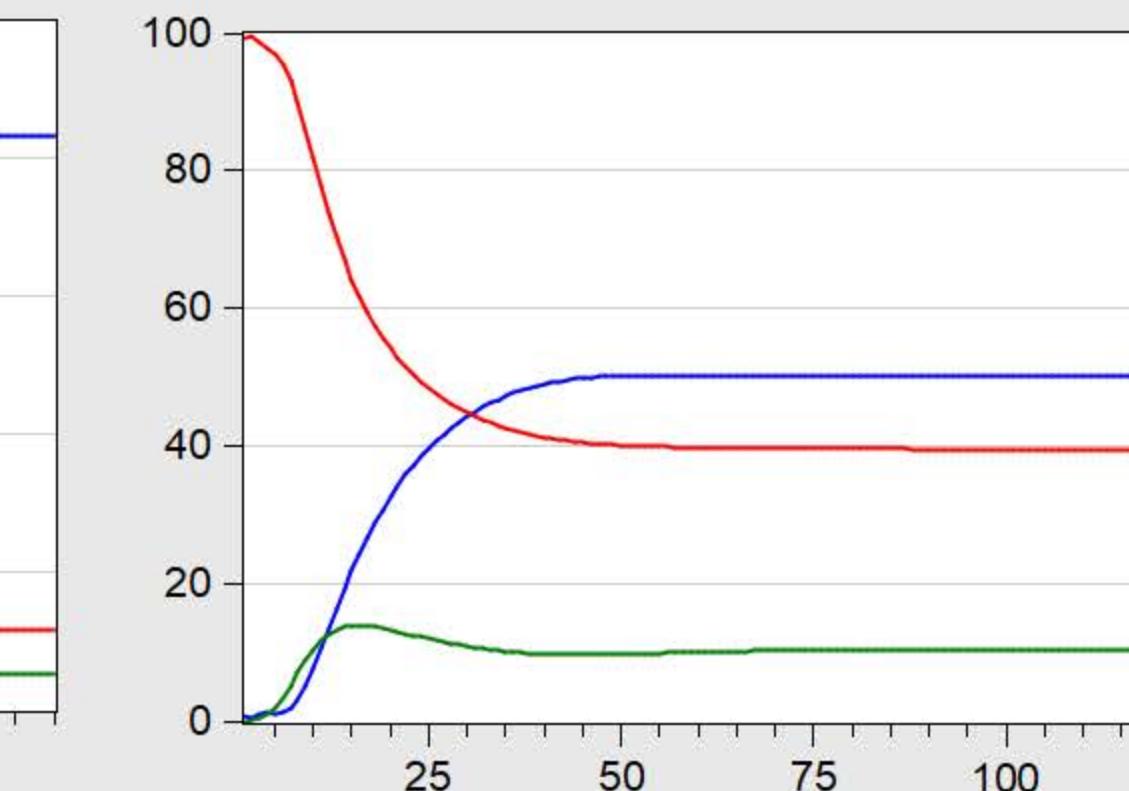
Variance Decomposition of R



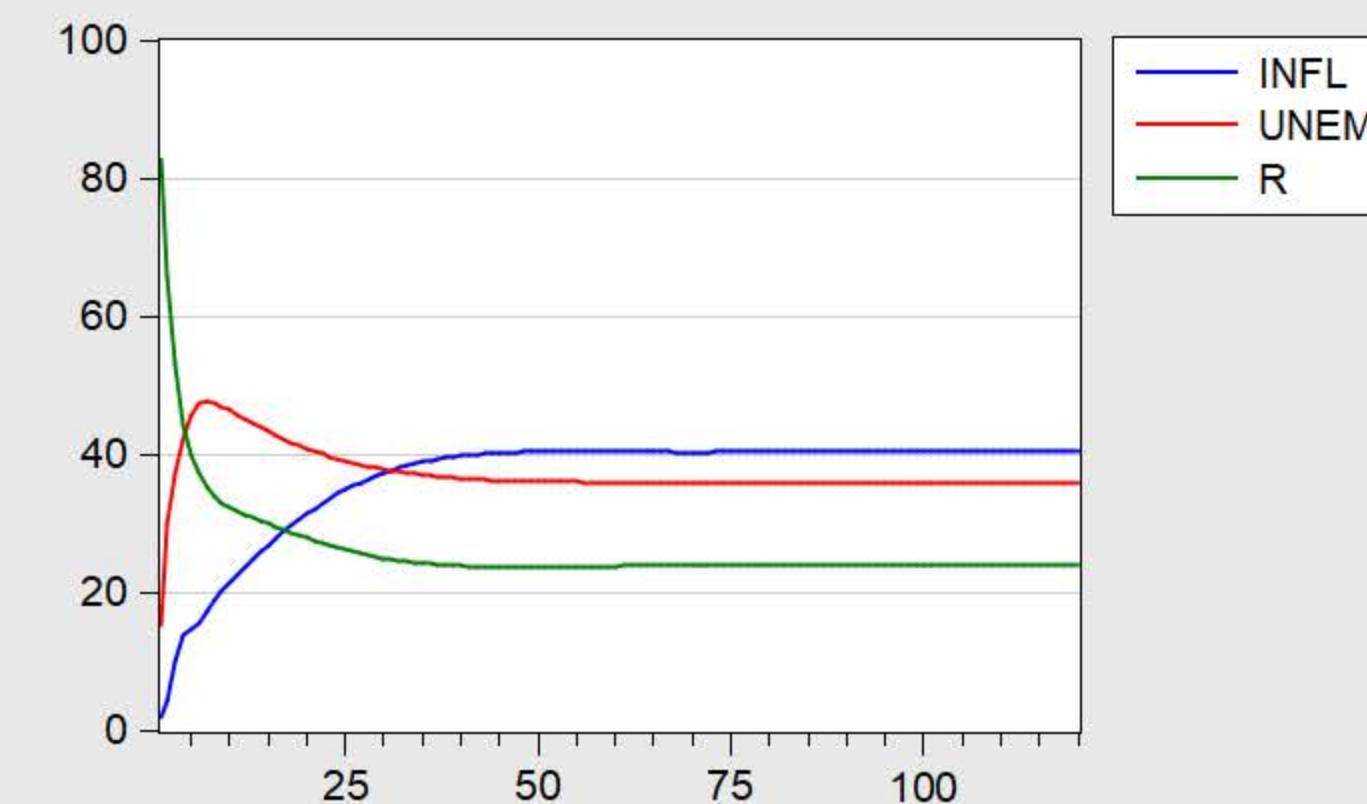
Variance Decomposition of INFL



Variance Decomposition of UNEMP



Variance Decomposition of R



*B. Variance Decompositions from the Recursive VAR Ordered as  $\pi$ ,  $u$ ,  $R$* *B.i. Variance Decomposition of  $\pi$* 

| Forecast<br>Horizon | Forecast<br>Standard Error | Variance Decomposition<br>(Percentage Points) |     |     |
|---------------------|----------------------------|---|-----|-----|
|                     |                            | $\pi$   | $u$ | $R$ |
| 1                   | 0.96                       | 100   | 0   | 0   |
| 4                   | 1.34                       | 88  | 10  | 2   |
| 8                   | 1.75                       | 82  | 17  | 1   |
| 12                  | 1.97                       | 82  | 16  | 2   |

*B.ii. Variance Decomposition of  $u$* 

| Forecast<br>Horizon | Forecast<br>Standard Error | Variance Decomposition<br>(Percentage Points) |     |     |
|---------------------|----------------------------|---|-----|-----|
|                     |                            | $\pi$   | $u$ | $R$ |
| 1                   | 0.23                       | 1   | 99  | 0   |
| 4                   | 0.64                       | 0   | 98  | 2   |
| 8                   | 0.79                       | 7   | 82  | 11  |
| 12                  | 0.92                       | 16  | 66  | 18  |

*B.iii. Variance Decomposition of  $R$* 

| Forecast<br>Horizon | Forecast<br>Standard Error | Variance Decomposition<br>(Percentage Points) |     |     |
|---------------------|----------------------------|---|-----|-----|
|                     |                            | $\pi$   | $u$ | $R$ |
| 1                   | 0.85                       | 2   | 19  | 79  |
| 4                   | 1.84                       | 9   | 50  | 41  |
| 8                   | 2.44                       | 12  | 60  | 28  |
| 12                  | 2.63                       | 16  | 59  | 25  |

*B. Variance Decompositions from the Recursive VAR Ordered as  $\pi$ ,  $u$ ,  $R$*

*B.i. Variance Decomposition of  $\pi$*

| <i>Forecast<br/>Horizon</i> | <i>Forecast<br/>Standard Error</i> | <i>Variance Decomposition<br/>(Percentage Points)</i> |     |     |
|-----------------------------|------------------------------------|---|-----|-----|
|                             |                                    | $\pi$   | $u$ | $R$ |
| 1                           | 0.96                               | 100   | 0   | 0   |
| 4                           | 1.34                               | 88  | 10  | 2   |
| 8                           | 1.75                               | 82  | 17  | 1   |
| 12                          | 1.97                               | 82  | 16  | 2   |

*B. Variance Decompositions from the Recursive VAR Ordered as  $\pi$ ,  $u$ ,  $R$* *B.i. Variance Decomposition of  $\pi$* 

| Forecast<br>Horizon | Forecast<br>Standard Error | Variance Decomposition<br>(Percentage Points) |     |     |
|---------------------|----------------------------|---|-----|-----|
|                     |                            | $\pi$   | $u$ | $R$ |
| 1                   | 0.96                       | 100   | 0   | 0   |
| 4                   | 1.34                       | 88  | 10  | 2   |
| 8                   | 1.75                       | 82  | 17  | 1   |
| 12                  | 1.97                       | 82  | 16  | 2   |

*B.ii. Variance Decomposition of  $u$* 

| Forecast<br>Horizon | Forecast<br>Standard Error | Variance Decomposition<br>(Percentage Points) |     |     |
|---------------------|----------------------------|---|-----|-----|
|                     |                            | $\pi$   | $u$ | $R$ |
| 1                   | 0.23                       | 1   | 99  | 0   |
| 4                   | 0.64                       | 0   | 98  | 2   |
| 8                   | 0.79                       | 7   | 82  | 11  |
| 12                  | 0.92                       | 16  | 66  | 18  |

*B.iii. Variance Decomposition of  $R$* 

| Forecast<br>Horizon | Forecast<br>Standard Error | Variance Decomposition<br>(Percentage Points) |     |     |
|---------------------|----------------------------|---|-----|-----|
|                     |                            | $\pi$   | $u$ | $R$ |
| 1                   | 0.85                       | 2   | 19  | 79  |
| 4                   | 1.84                       | 9   | 50  | 41  |
| 8                   | 2.44                       | 12  | 60  | 28  |
| 12                  | 2.63                       | 16  | 59  | 25  |